

Polarimetric Camera Calibration Using an LCD Monitor

Zhixiang Wang

Supervisor: Yung-Yu Chuang, Ph.D.

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CALIFORNIA
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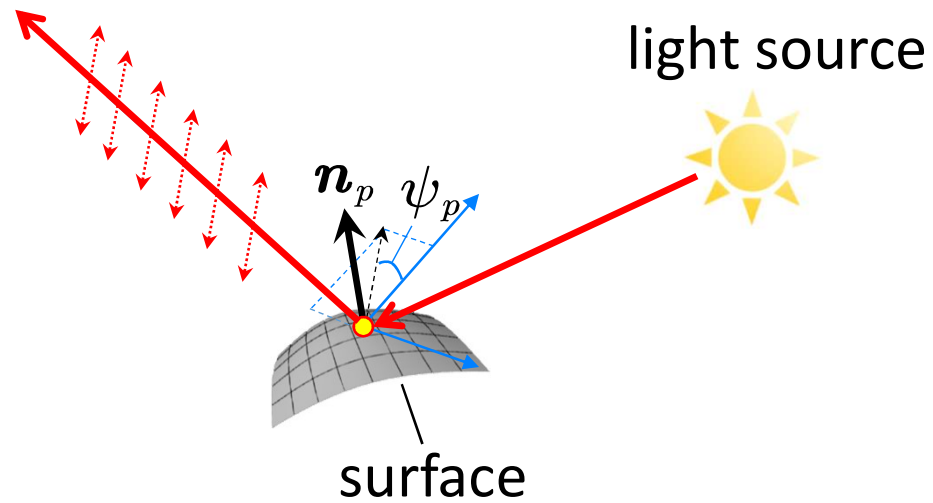


國立臺灣大學
National Taiwan University

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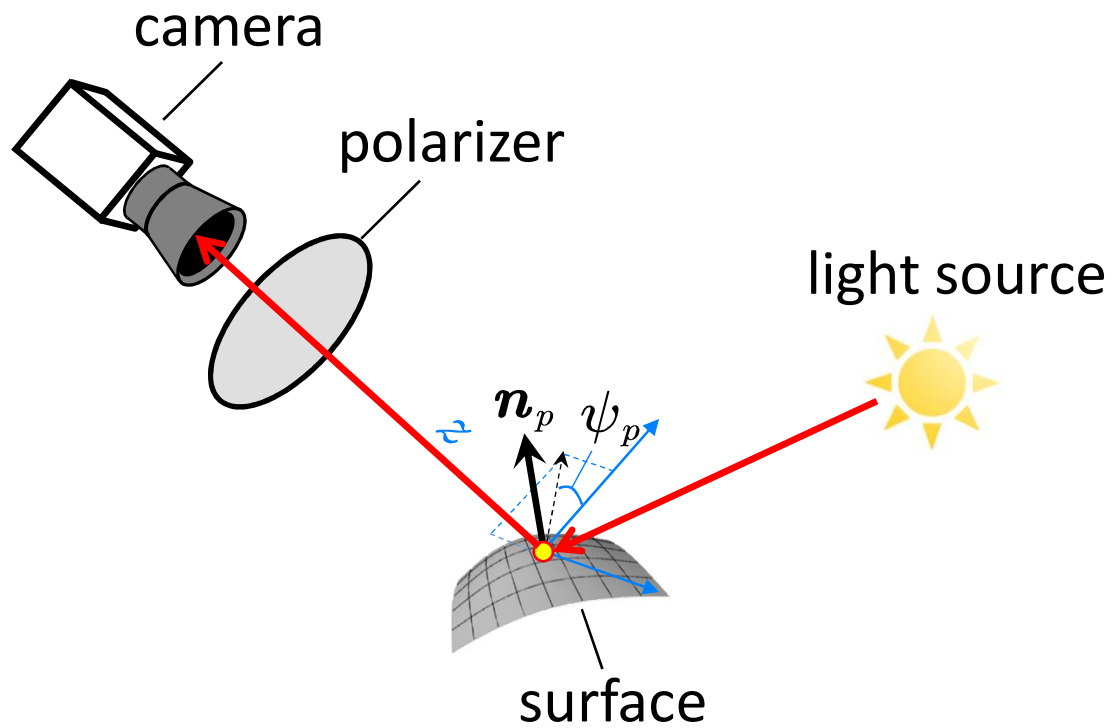
Polarization



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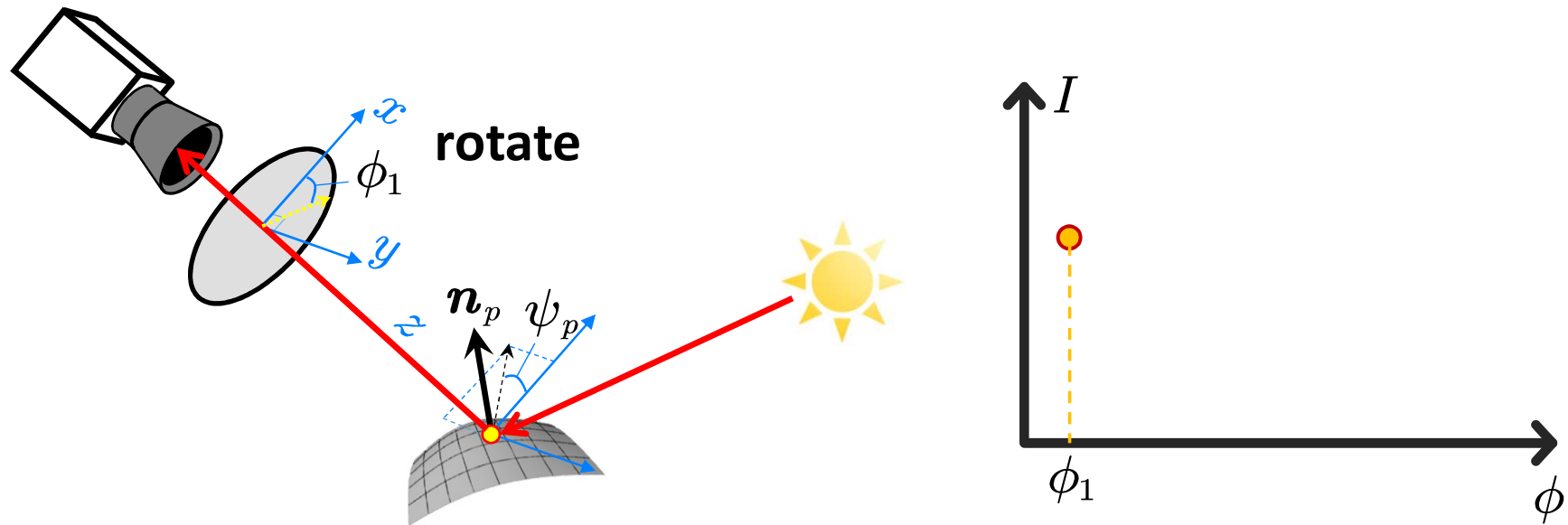
Polarization Imaging



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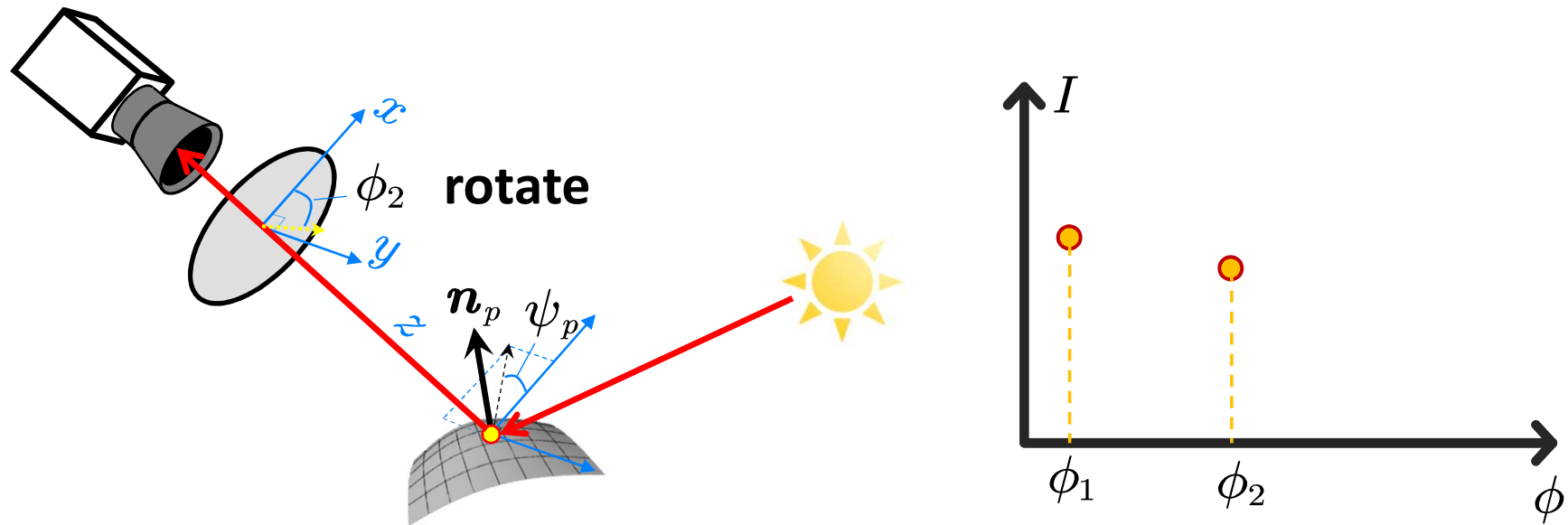
Polarization Imaging



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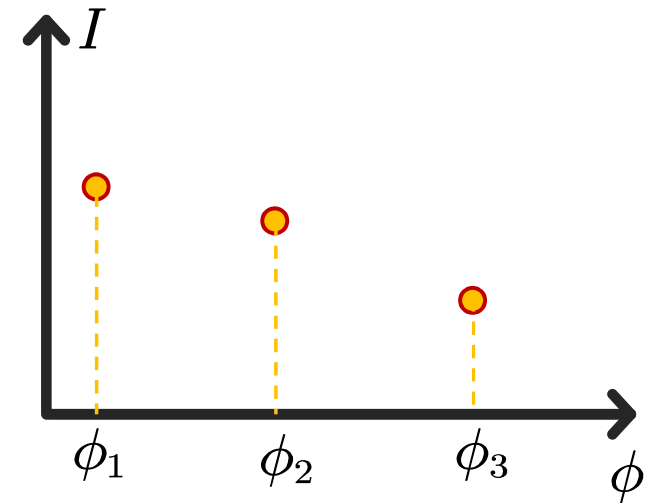
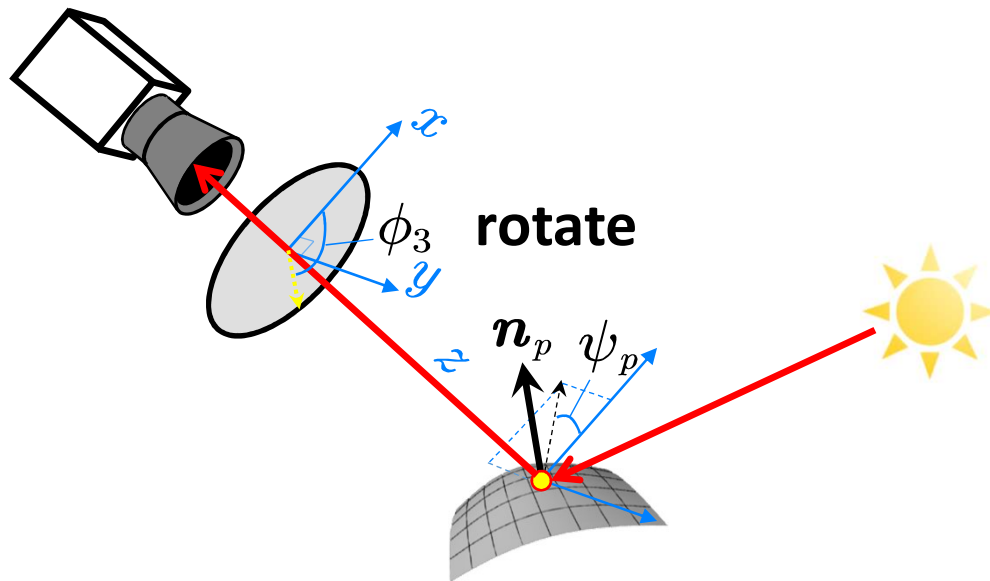
Polarization Imaging



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Polarization Imaging

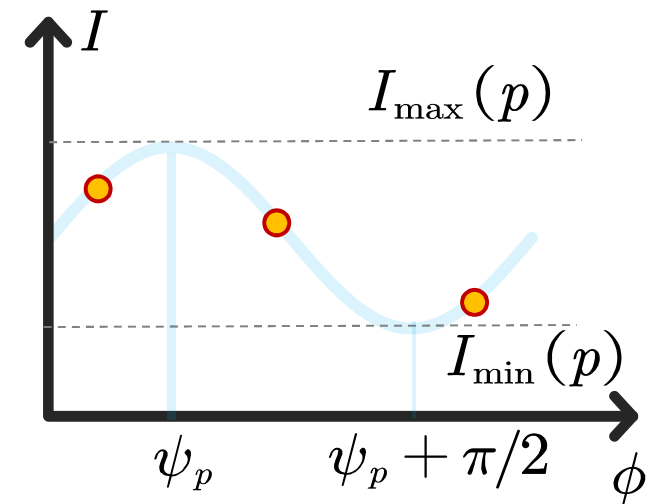
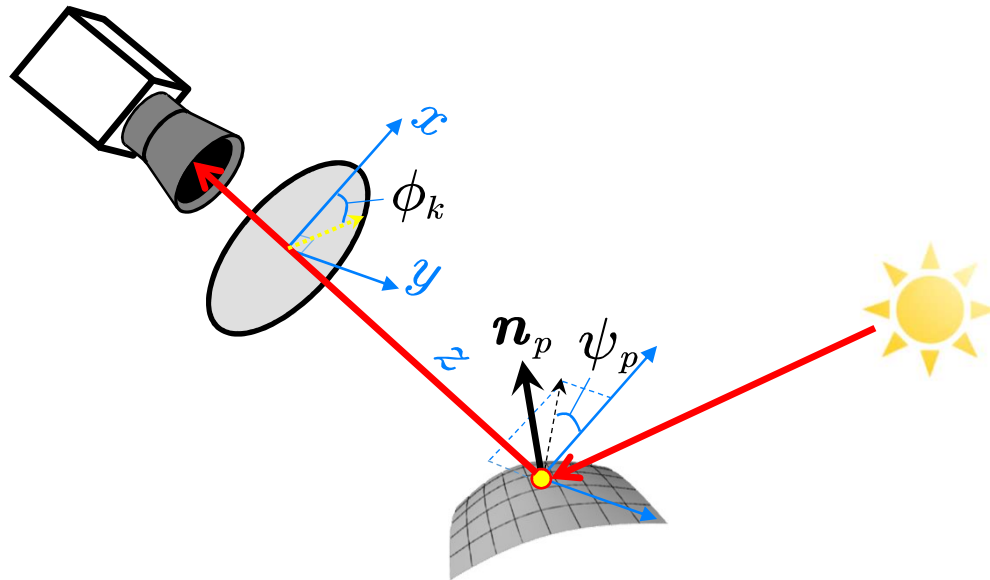


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Polarization Imaging

$$I_{k,p} = t_p + a_p \cos[2(\phi_k - \psi_p)]$$

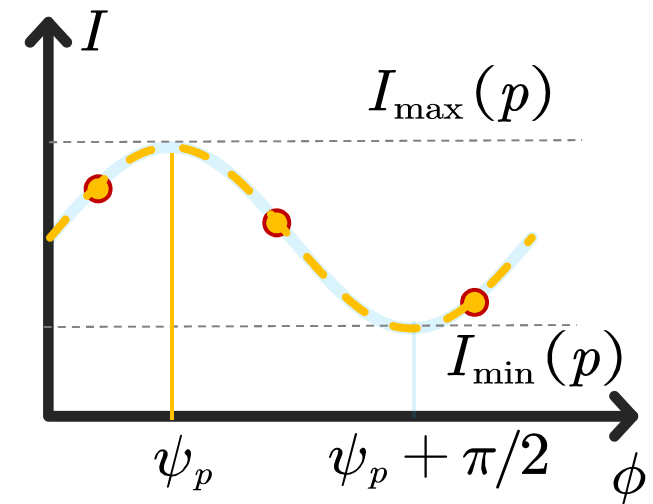
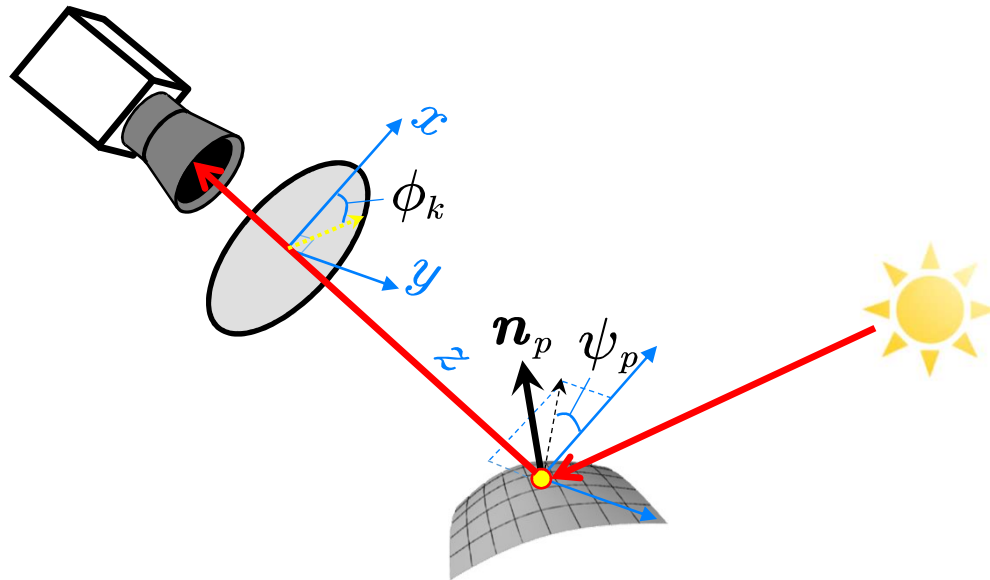


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Polarization Imaging

$$I_{k,p} = t_p + a_p \cos[2(\phi_k - \psi_p)]$$

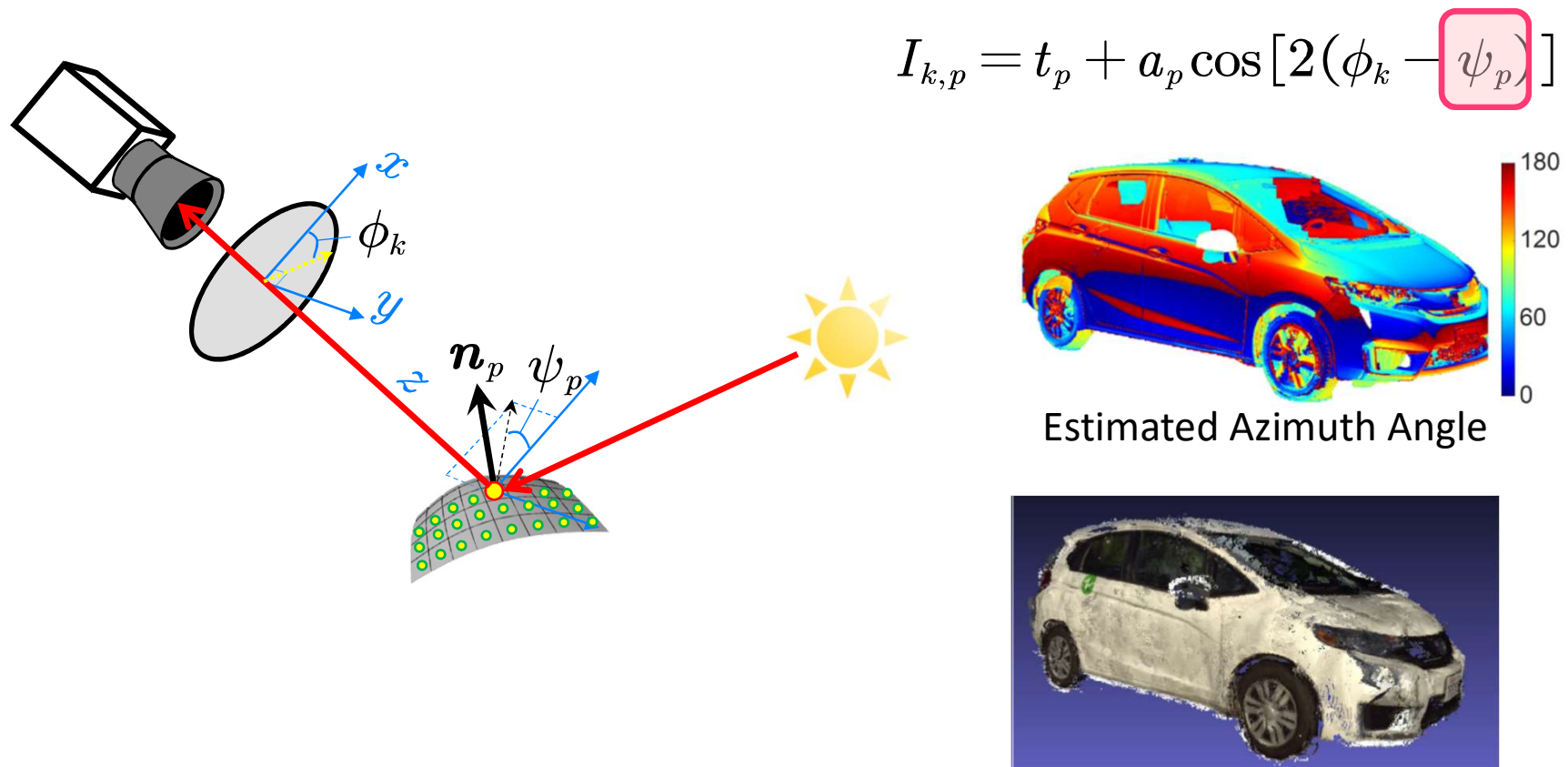


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Polarization Imaging

Shape from Polarization



[Miyazaki et al. PAMI'04] [Saito et al. CVPR'99]

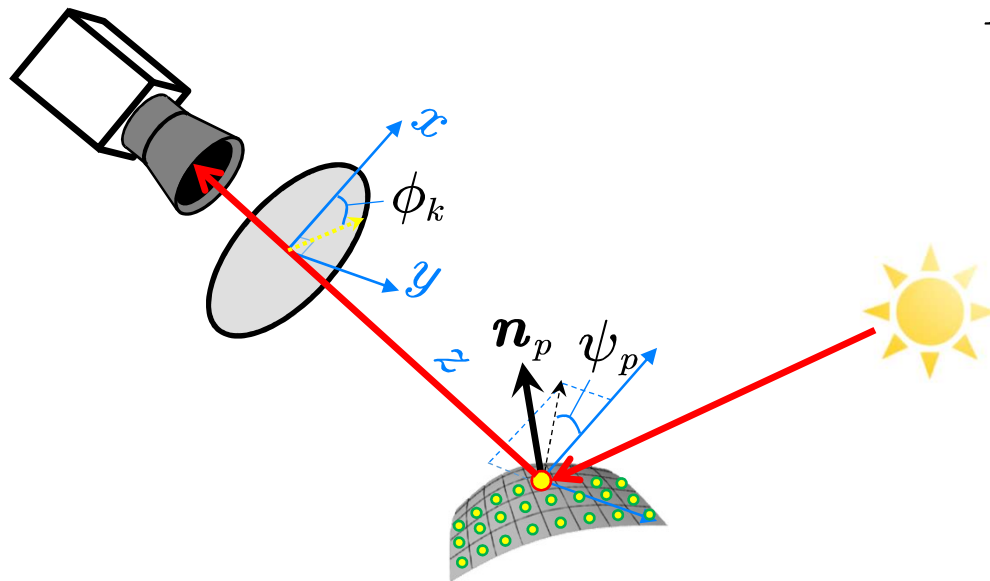
[Smith et al. ECCV'16] [Yu et al. ICCV'17]

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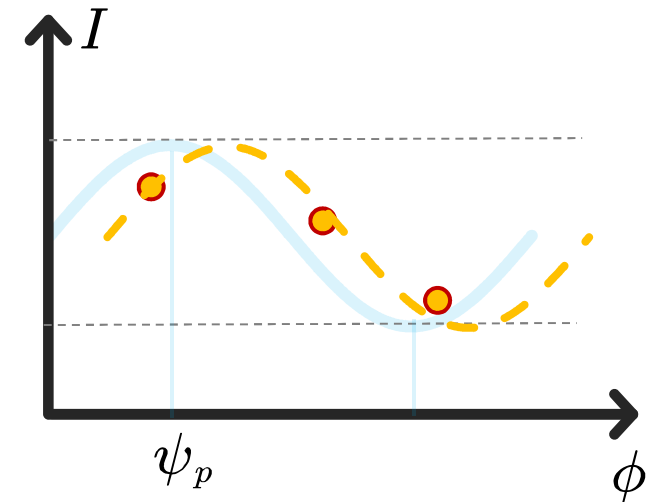
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Polarization Imaging

Shape from Polarization



$$I_{k,p} = t_p + a_p \cos[2(\phi_k - \psi_p)]$$



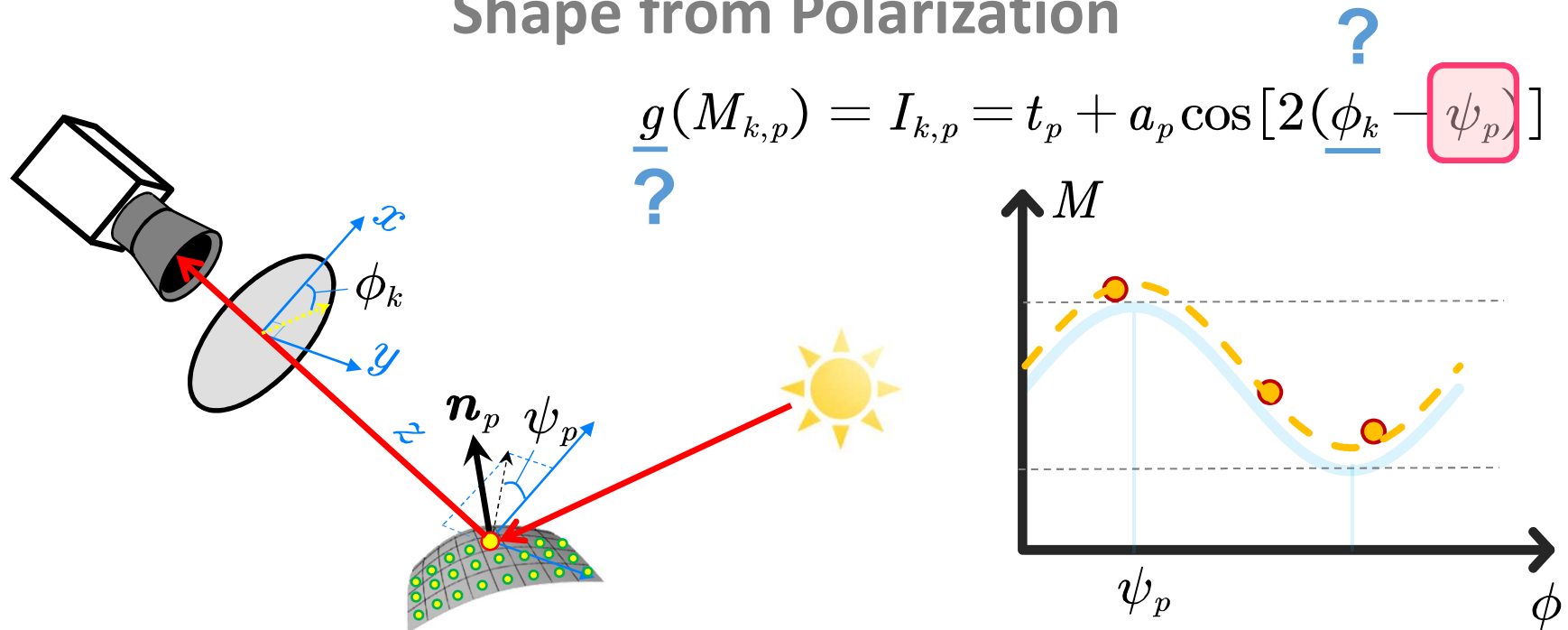
Challenges: - unknown polarimetry

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Polarization Imaging

Shape from Polarization



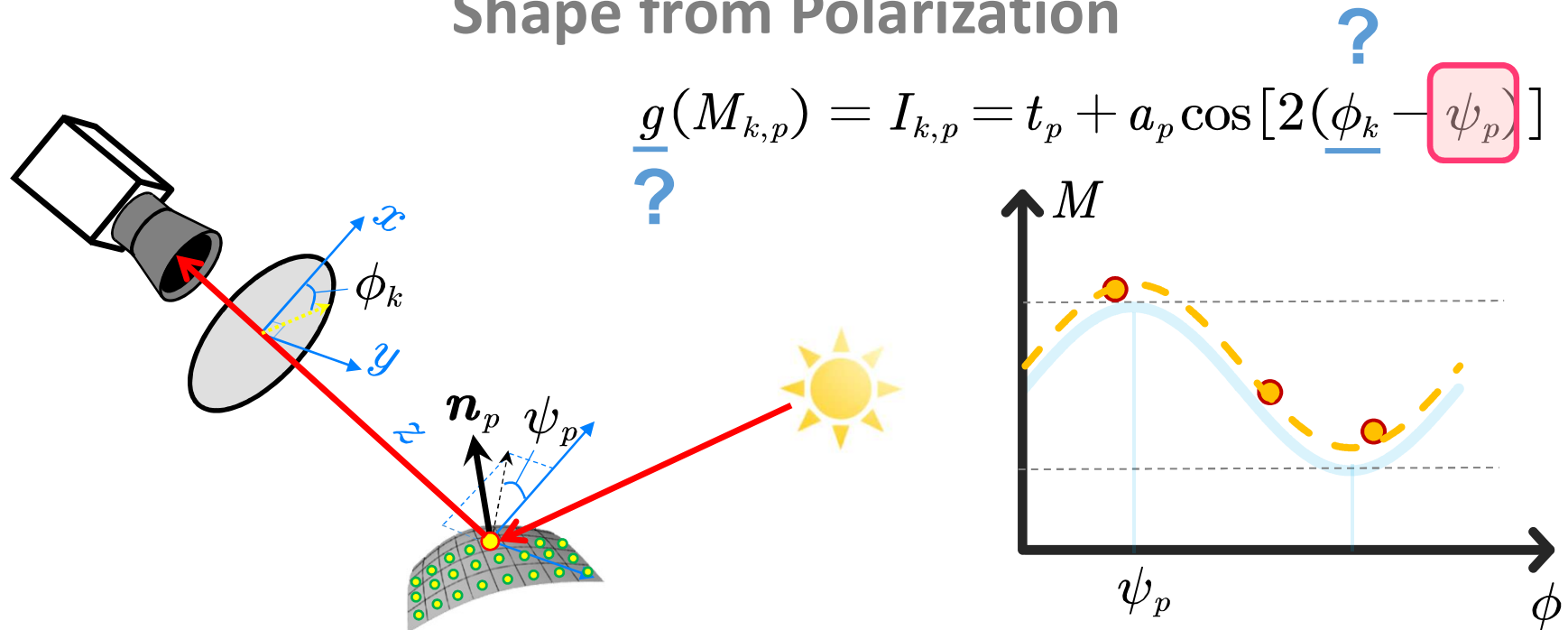
Challenges: - unknown polarimetry + radiometry

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Polarization Imaging

Shape from Polarization



Challenges: - unknown polarimetry + radiometry

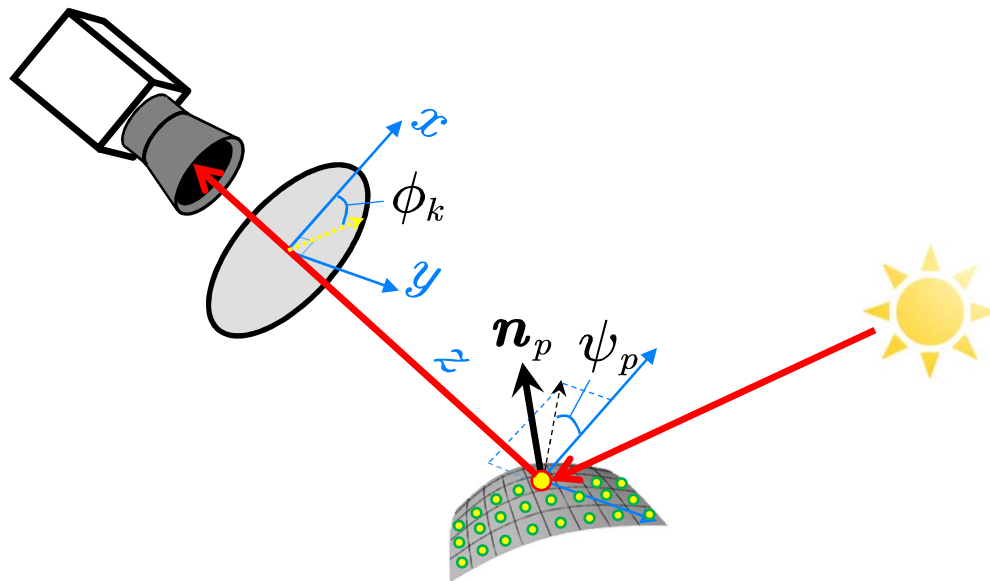
Calibration

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Polarization Imaging

Shape from Polarization



$$\cos[2(\phi_k - (\psi_p + \pi))]$$



$$\cos[2(\phi_k - \psi_p)]$$

Challenges: - unknown polarimetry + radiometry
- **ambiguity**

Calibration

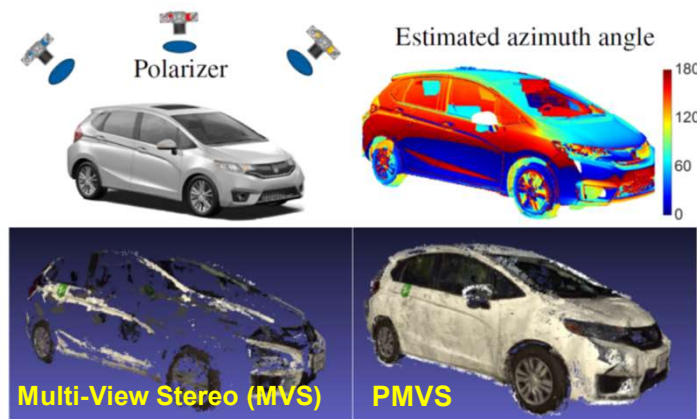
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Polarization Imaging

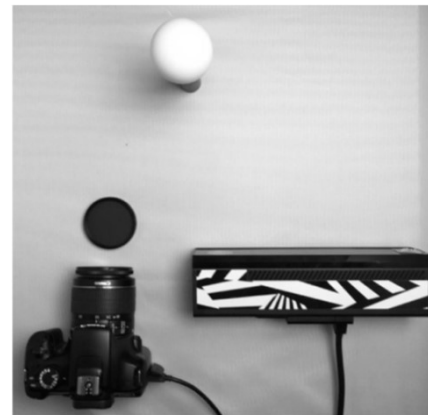
Solve Ambiguity

+ Multi-View Stereo



[Cui et al. CVPR'17]

+ Depth Sensors



[Kadambi et al. IJCV'17]

+ Binocular Stereo



[Berger et al. ICRA'17]

Challenges: - unknown polarimetry + radiometry

Calibration

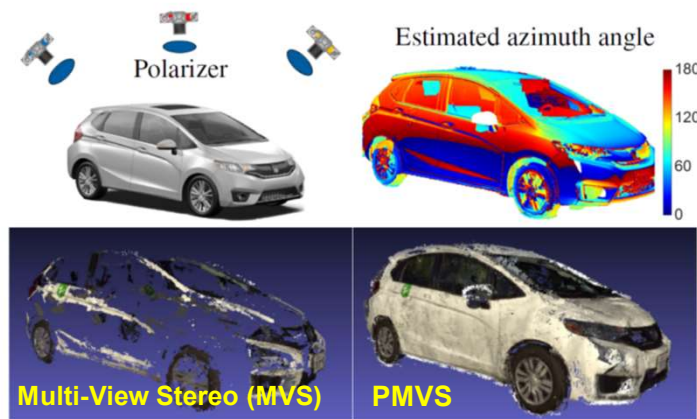
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Polarization Imaging

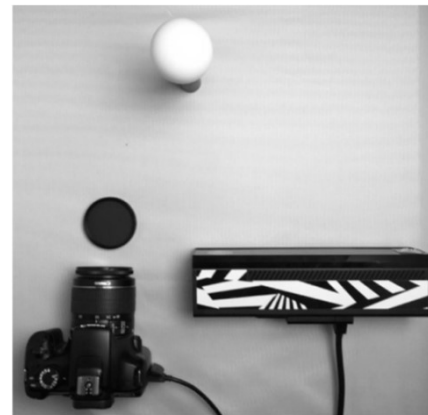
Solve Ambiguity

+ Multi-View Stereo



[Cui et al. CVPR'17]

+ Depth Sensors



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+ Binocular Stereo



[Berger et al. ICRA'17]

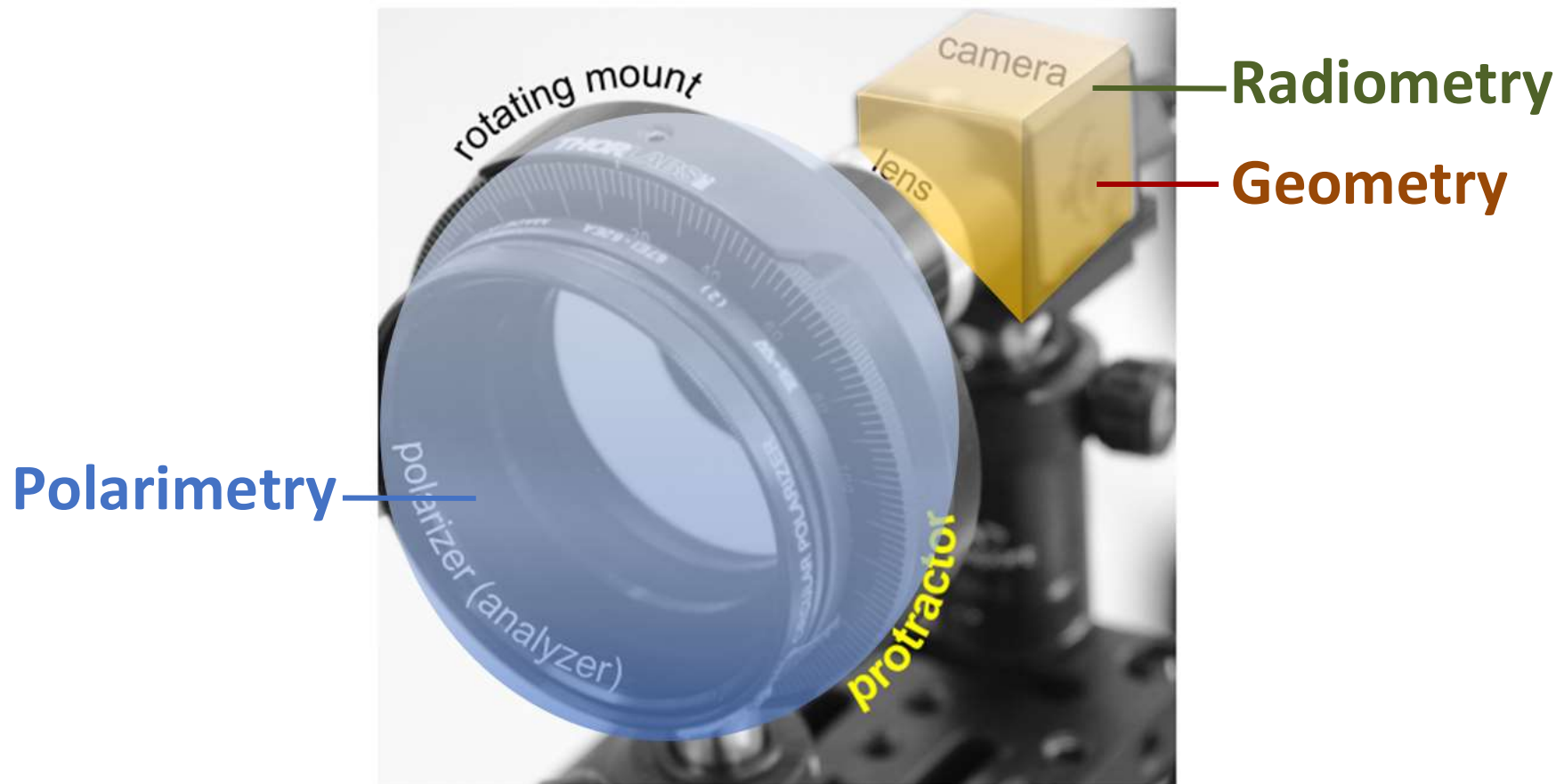
Challenges: - **unknown** polarimetry + radiometry
- require extra geometric parameters

Calibration

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Goal: Calibrate a polarimetric camera



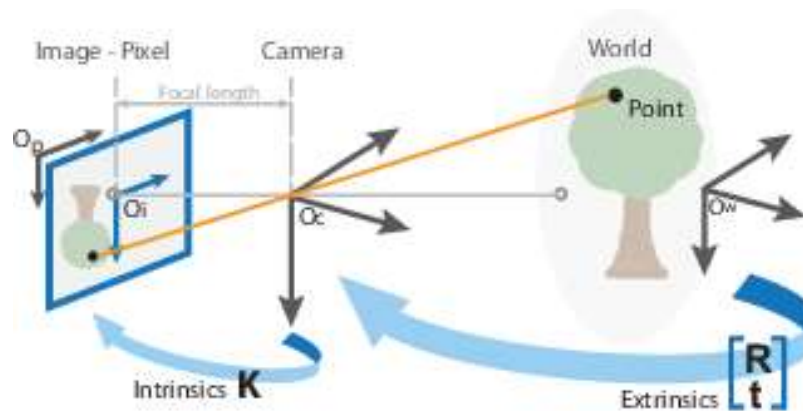
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Goal: Calibrate a polarimetric camera



Geometry

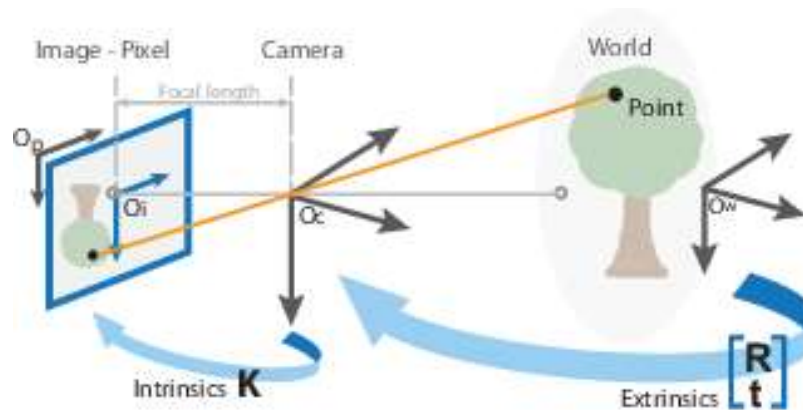


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Goal: Calibrate a polarimetric camera



Geometry



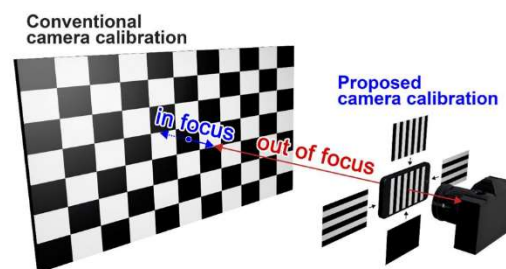
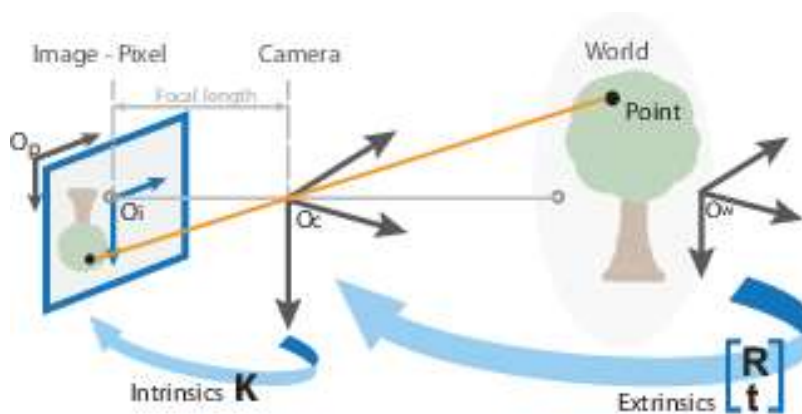
[Zhang et al. PAMI'00]

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Goal: Calibrate a polarimetric camera



Geometry



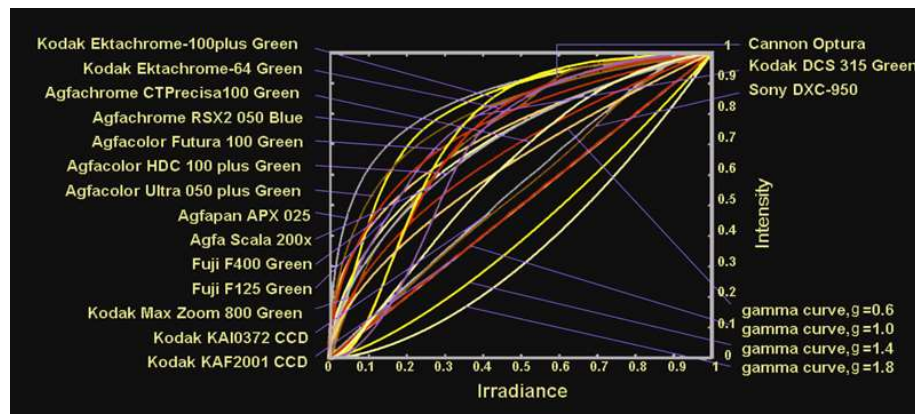
[Ha et al. ICCV'15]

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Goal: Calibrate a polarimetric camera



Radiometry

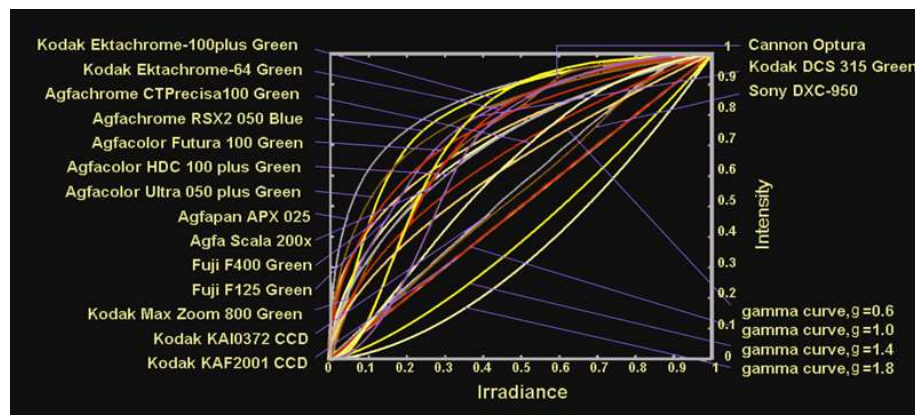


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Goal: Calibrate a polarimetric camera



Radiometry



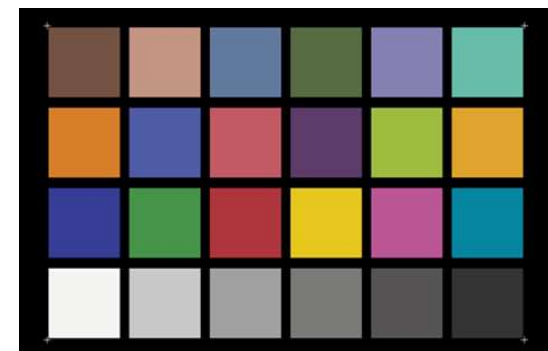
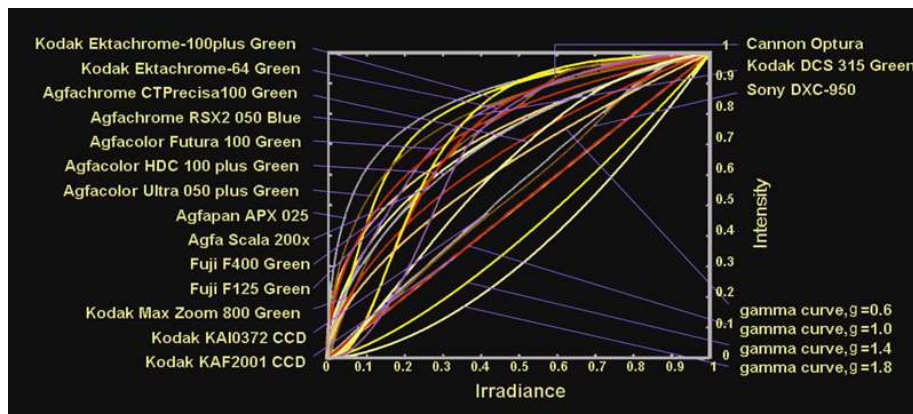
[Debevec et al. Siggraph'97]

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Goal: Calibrate a polarimetric camera



Radiometry

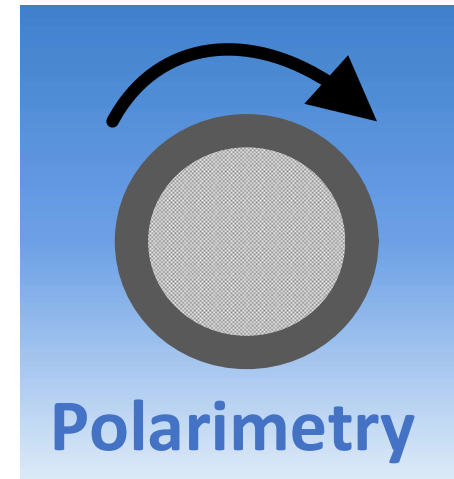


[McCamy et al. 76]

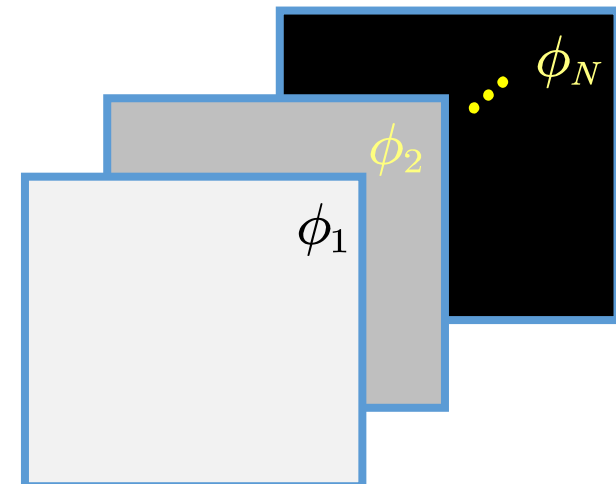
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Goal: Calibrate a polarimetric camera



$$I_{k,p} = t_p + a_p \cos [2(\phi_k - \psi_p)]$$



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Main idea: Using an LCD monitor



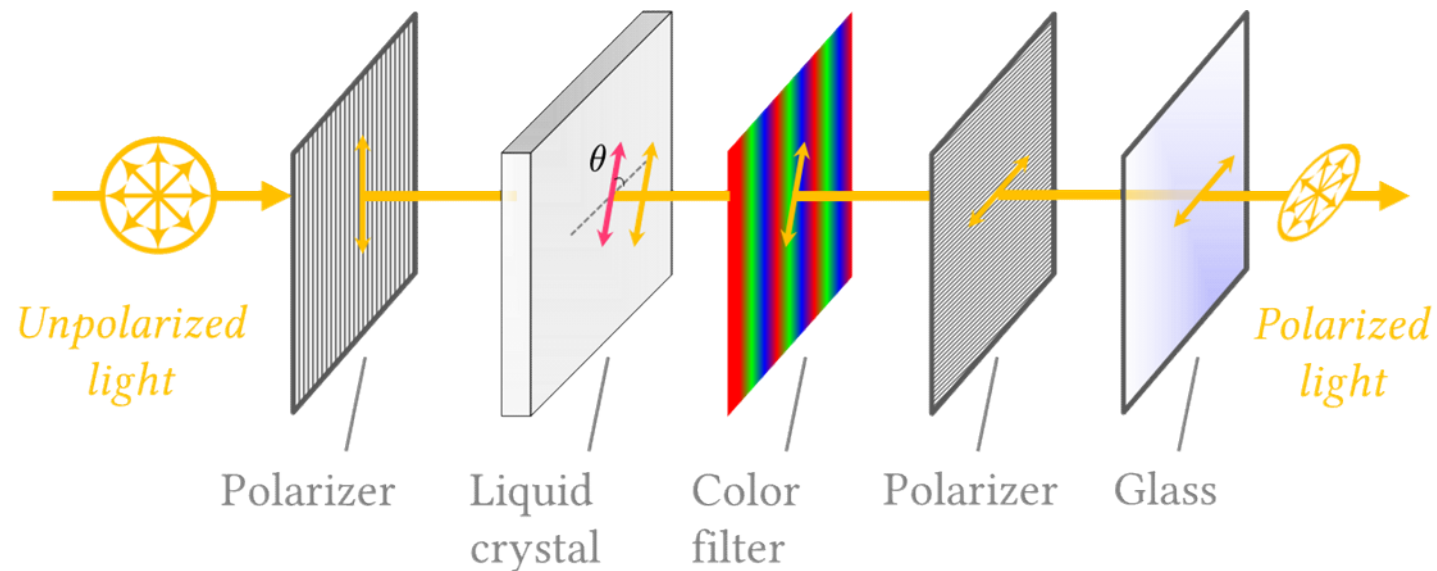
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Main idea: Using an LCD monitor



Typical interior structure of LCD monitors

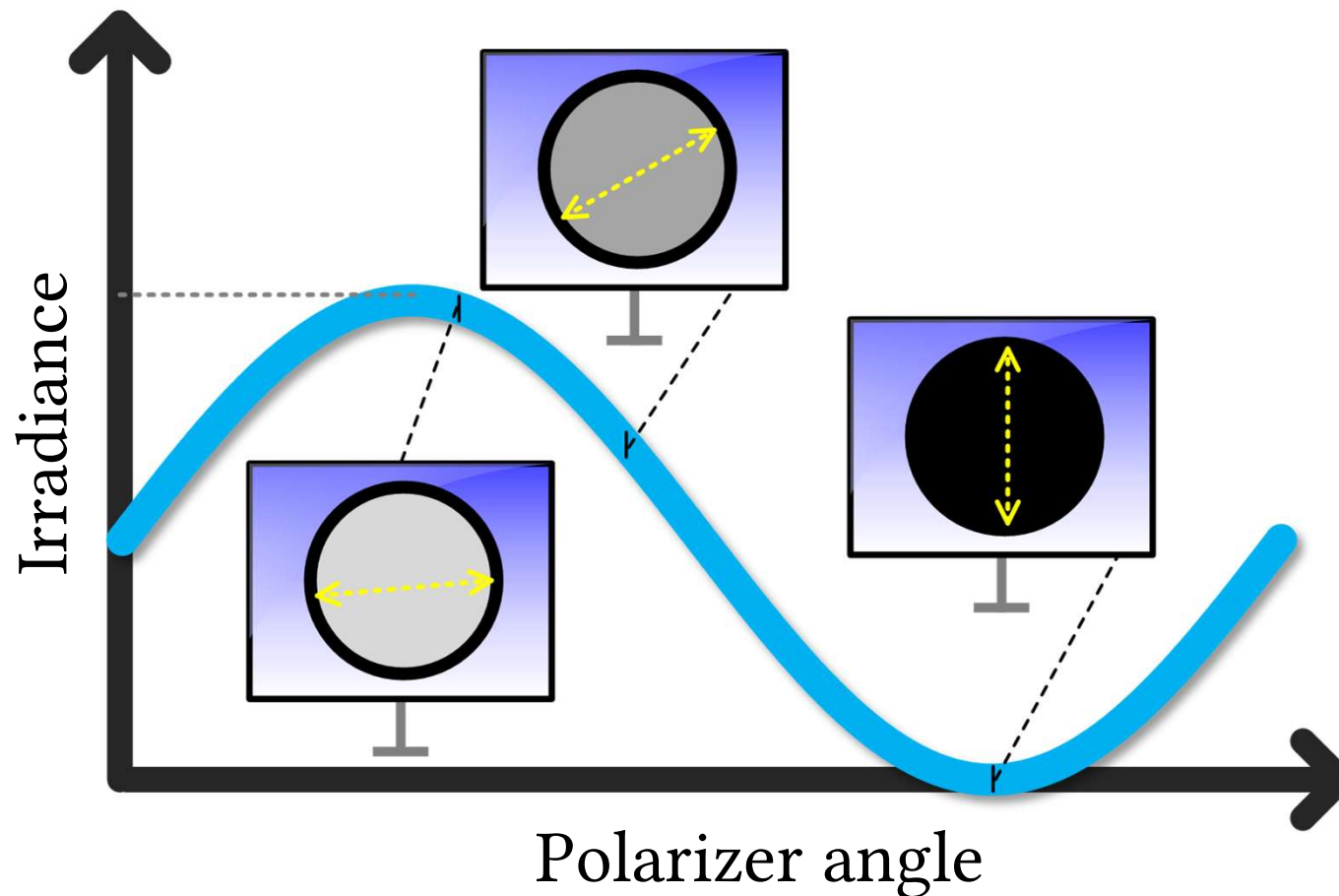


Introduction – Motivation

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LCD monitors

Viewed by a polarimetric camera

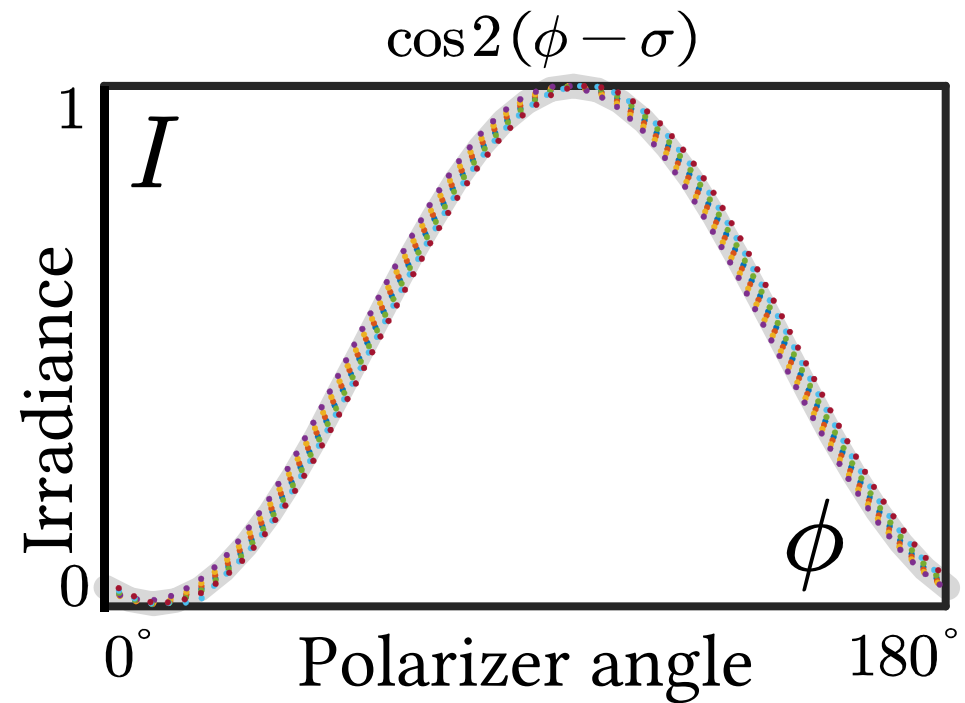
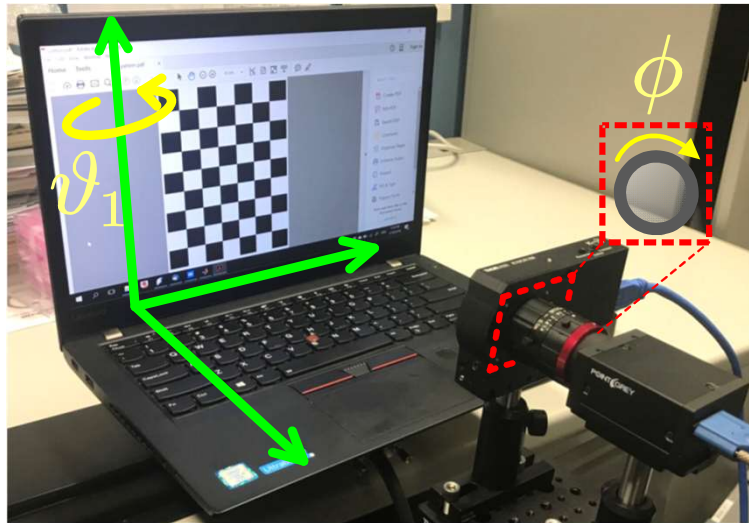


Introduction – Motivation

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LCD monitors

Characteristics A. In-plane rotation

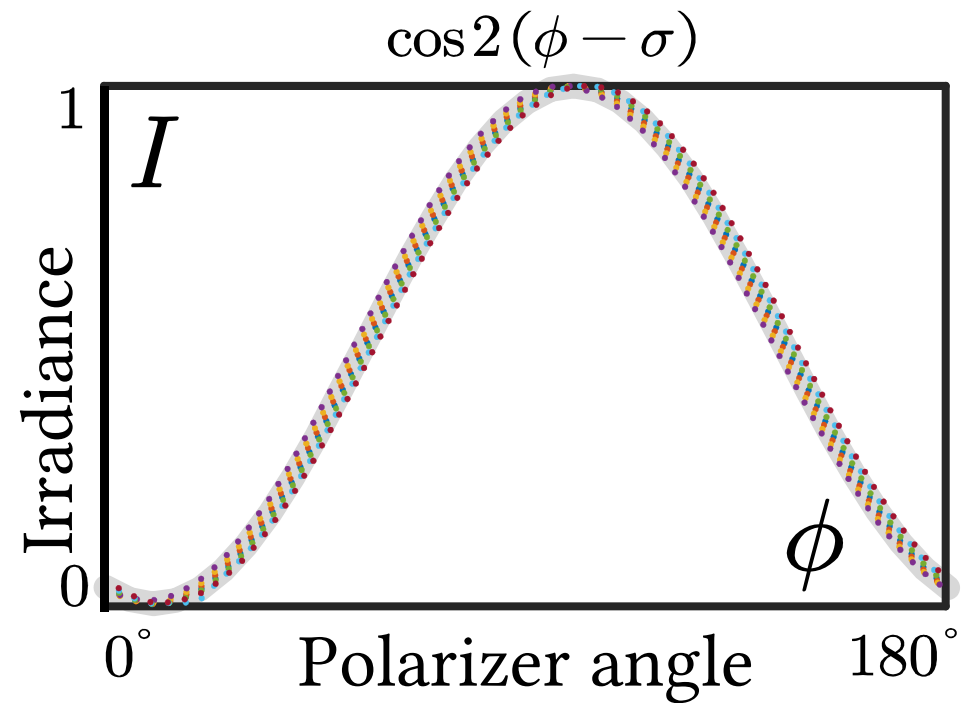
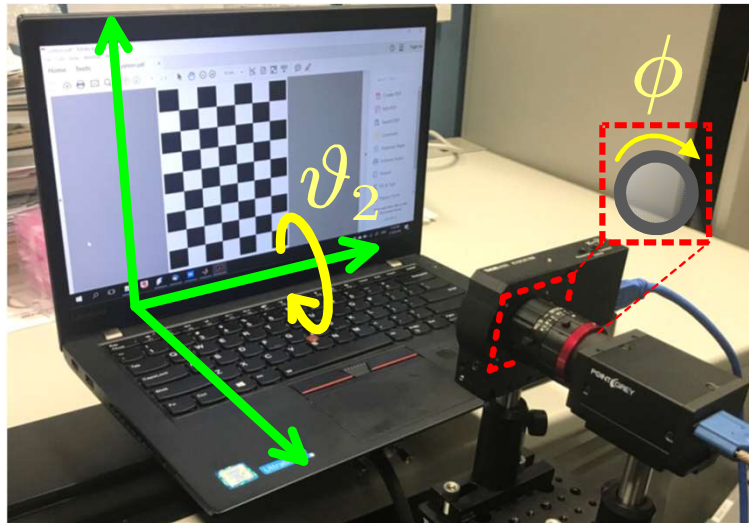


Introduction – Motivation

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LCD monitors

Characteristics A. In-plane rotation

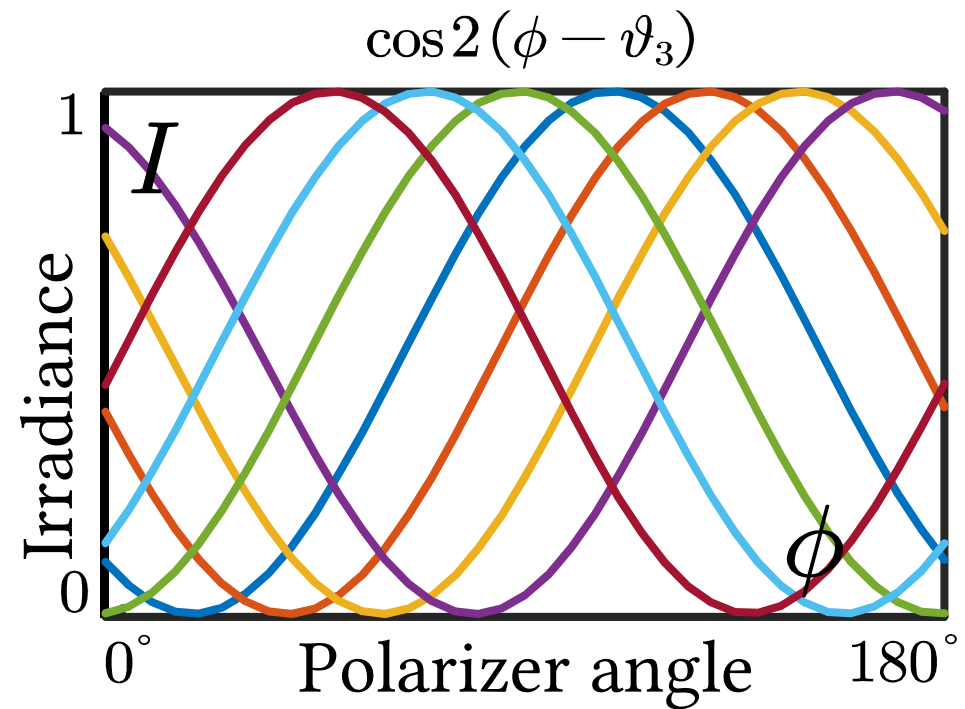
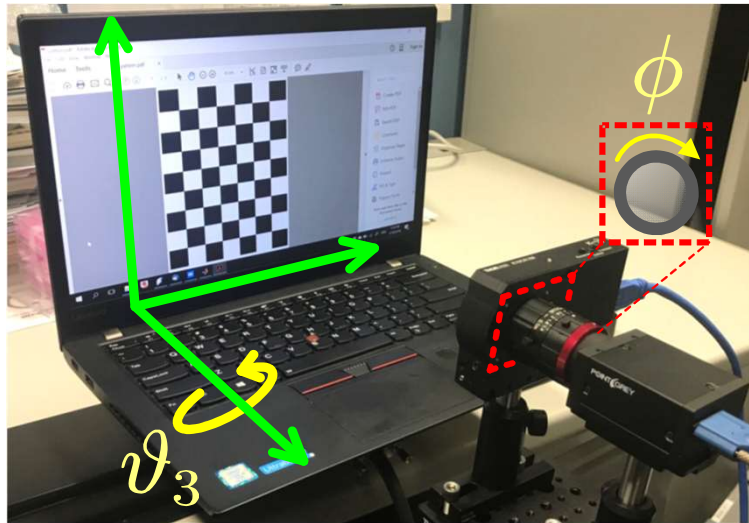


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LCD monitors

Characteristics A. In-plane rotation

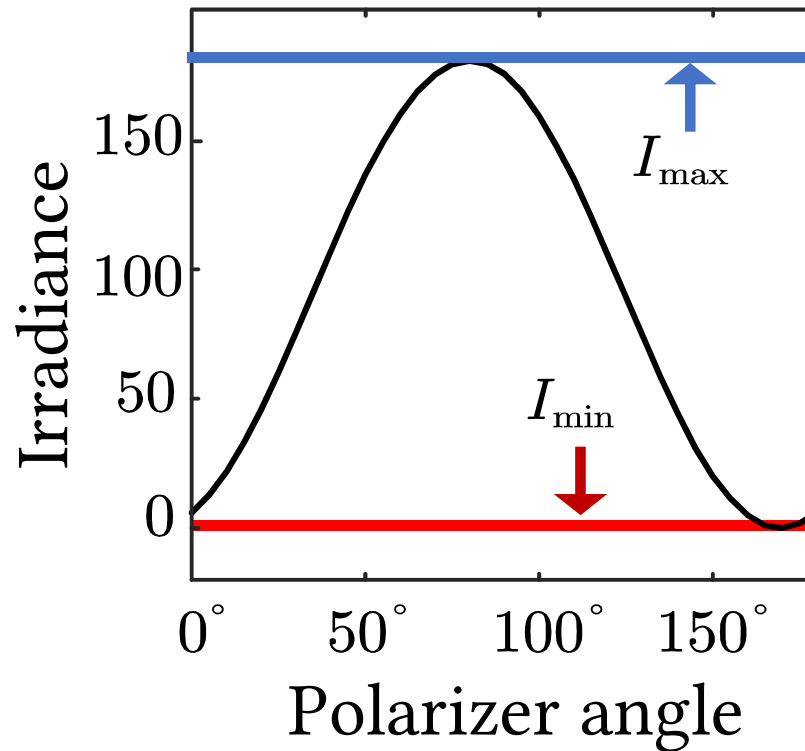


Introduction – Motivation

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LCD monitors

Characteristics B. Complete linear polarization



$$I_{\max} \gg I_{\min}$$

Introduction – Motivation

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Pattern-based calibration

	Is easy to select points?	Can work ≤ 3 polar channels?	Is robust to nonlinear CRF?	Is robust to initialization?	Radiometry?	Geometry?
self-calibration						
ICCP'15	✗	✗	✗	✗	✗	✗
CVPR'18	✗	✗	✗	✗	✓	✗
Ours	✓	✓	✓	✓	✓	✓

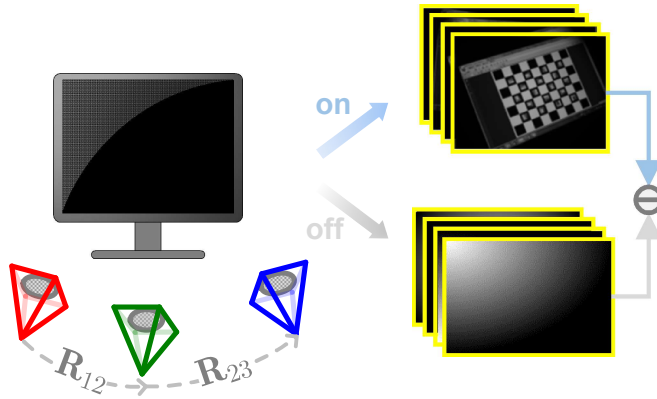
$$g(M_{k,p}) = I_{k,p} = t_p + a_p \cos[2(\phi_k - \psi_p)]$$

[Schechner et al. ICCP'15]

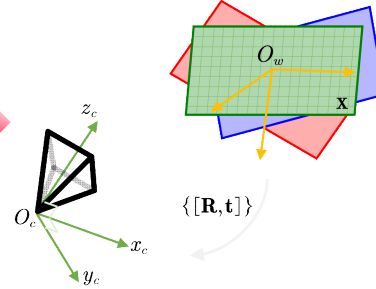
[Teo et al. CVPR'18]

Overview

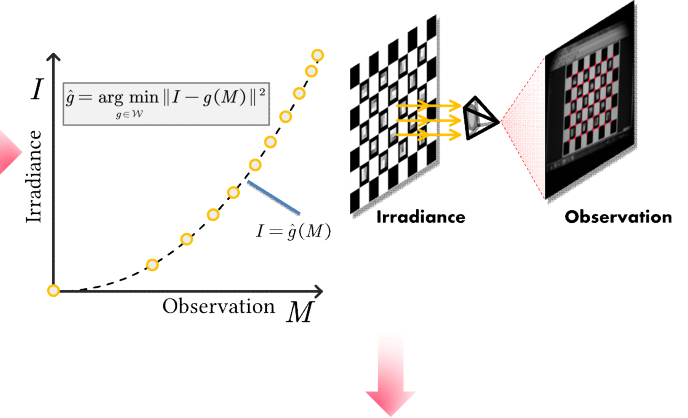
Step 1. Capture images



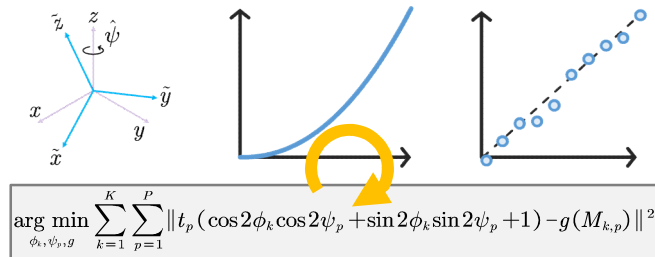
Step 2. Calibrate geometry



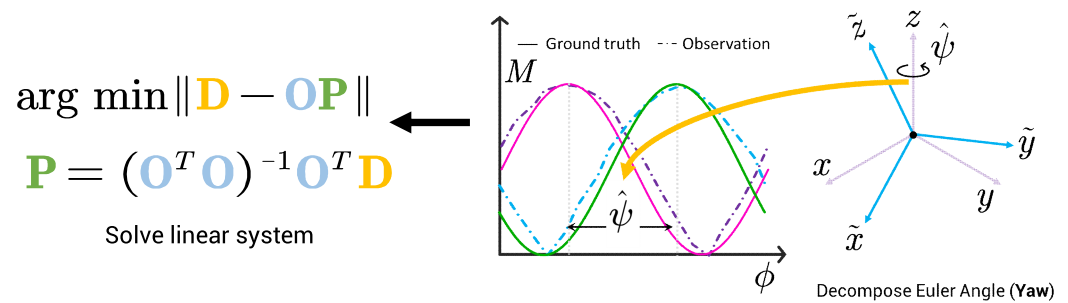
Step 3. Calibrate radiometry



Step 5. Bundle adjustment



Step 4. Calibrate polarimetry



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$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

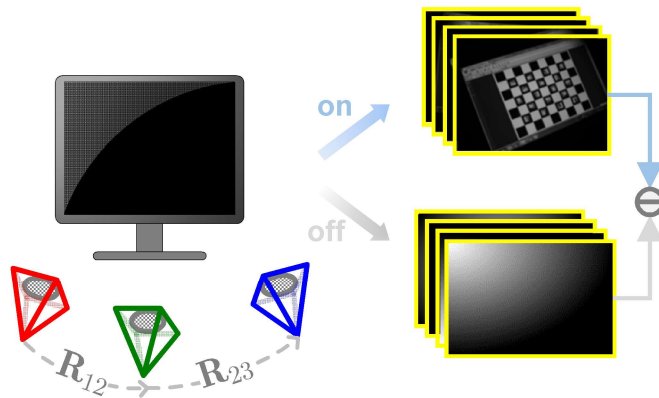
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??

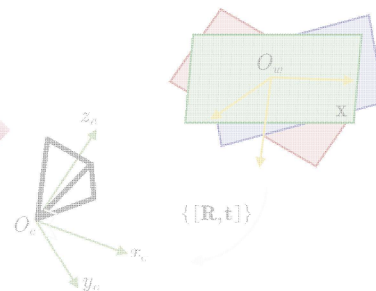
? ?

Overview

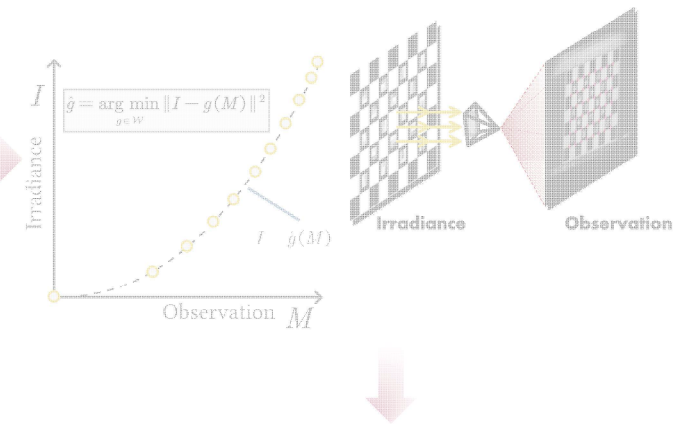
Step 1. Capture images



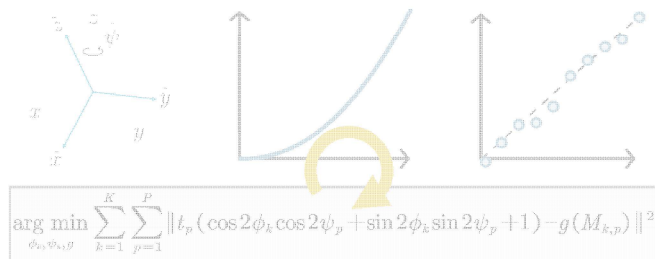
Step 2. Calibrate geometry



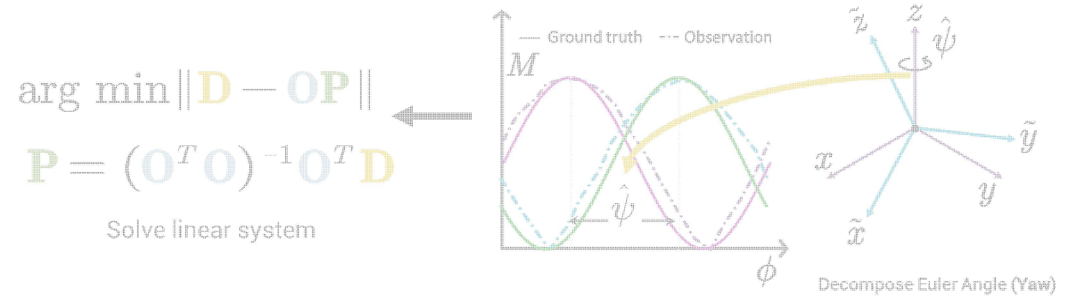
Step 3. Calibrate radiometry



Step 5. Bundle adjustment

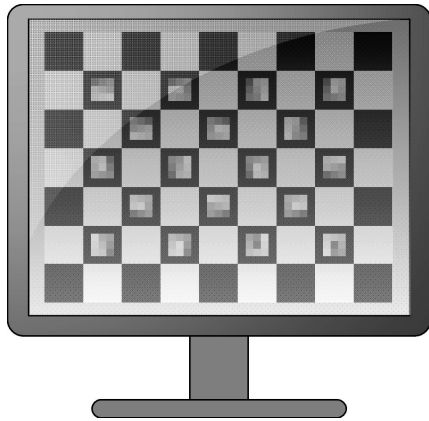


Step 4. Calibrate polarimetry



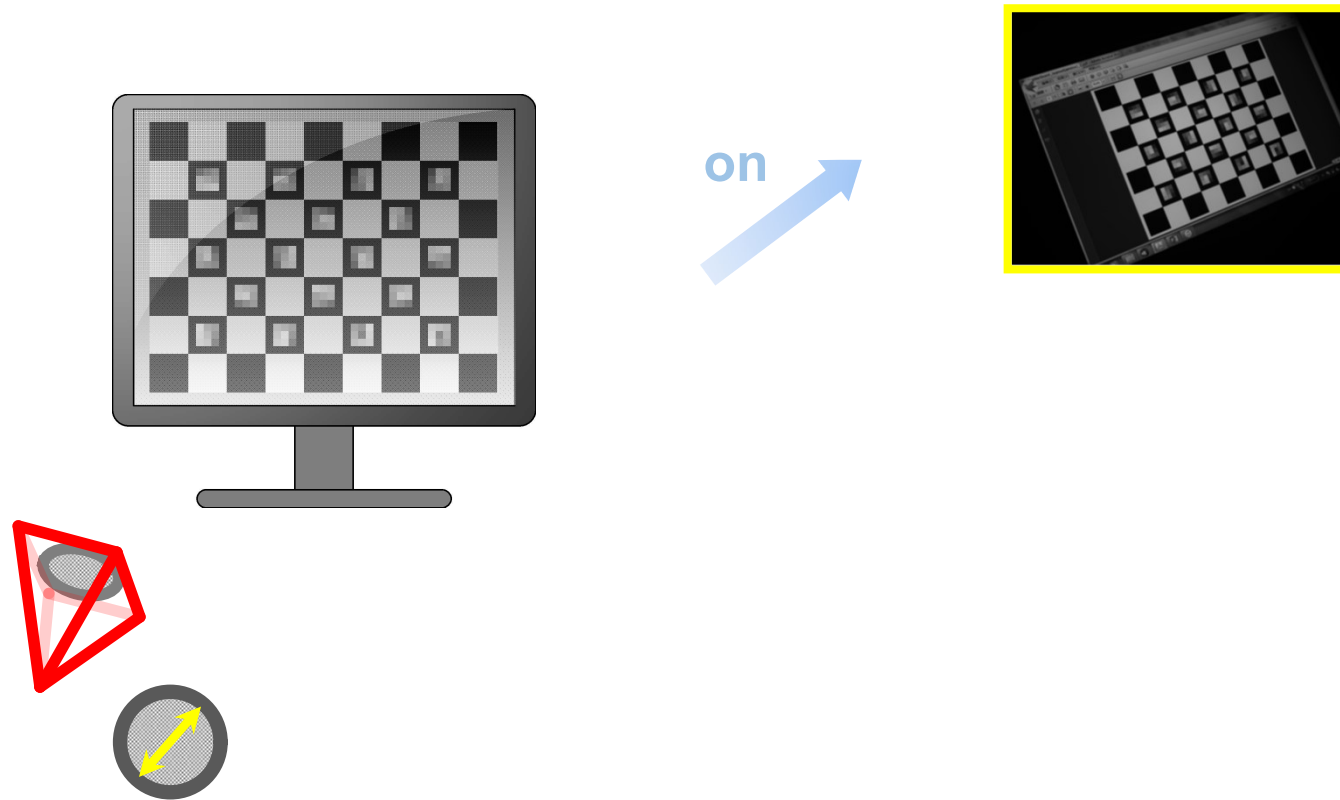
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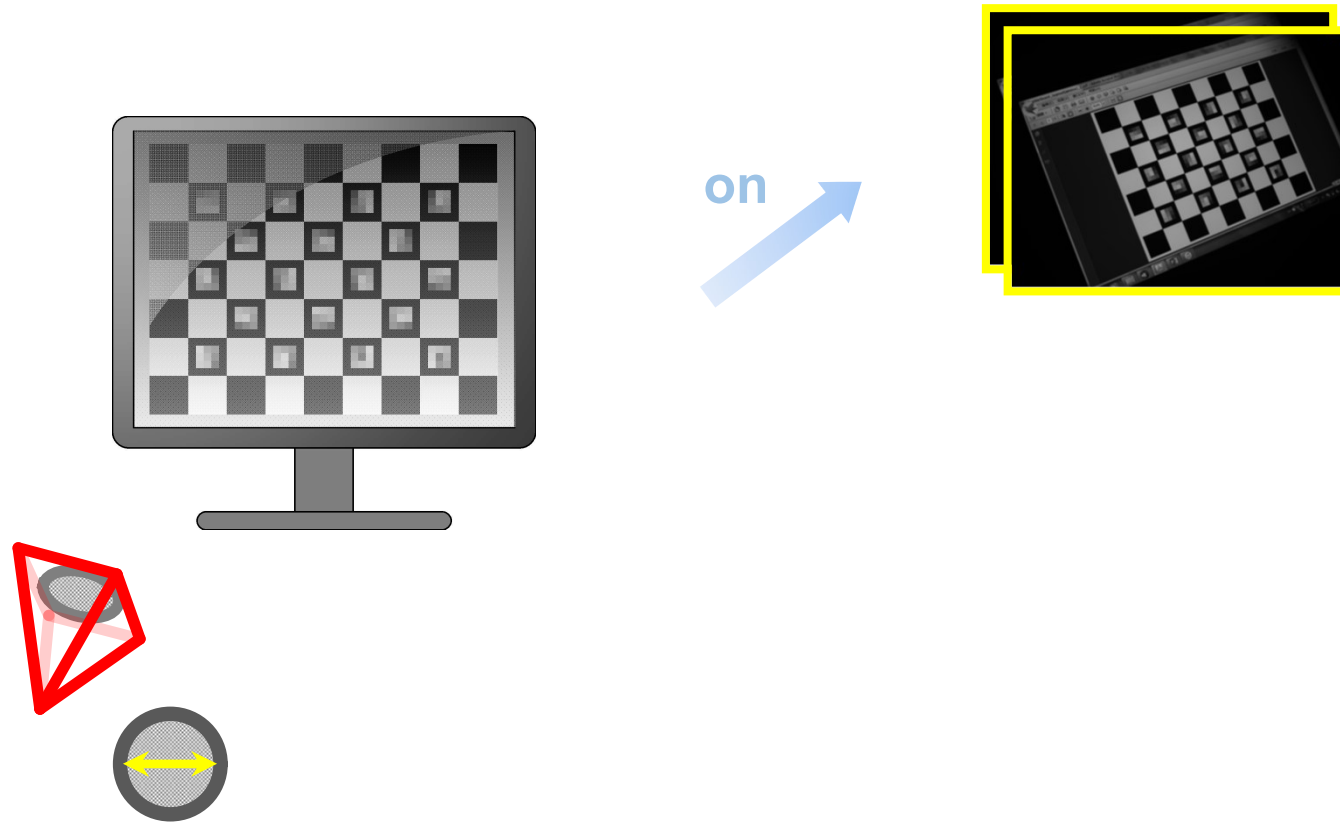
Method

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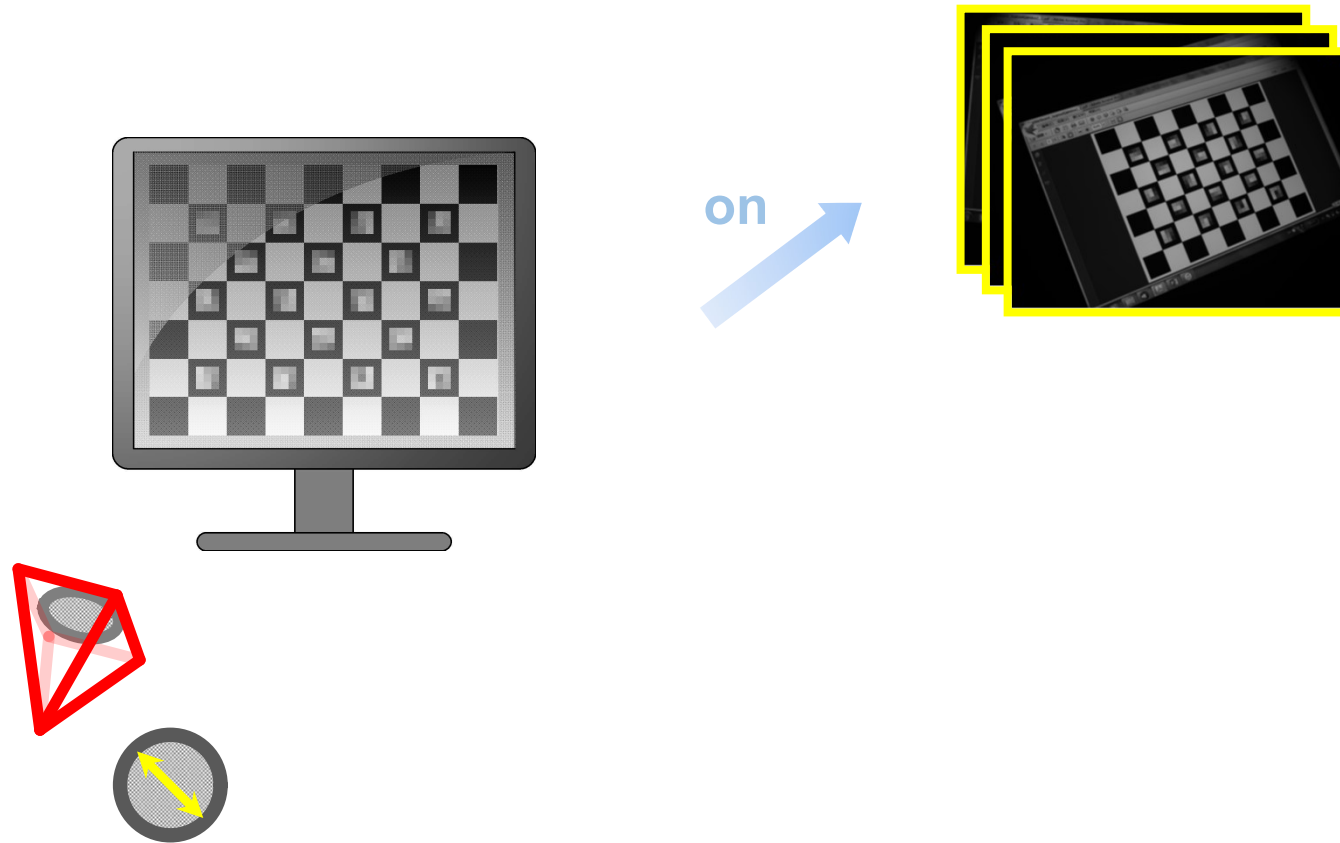
Method

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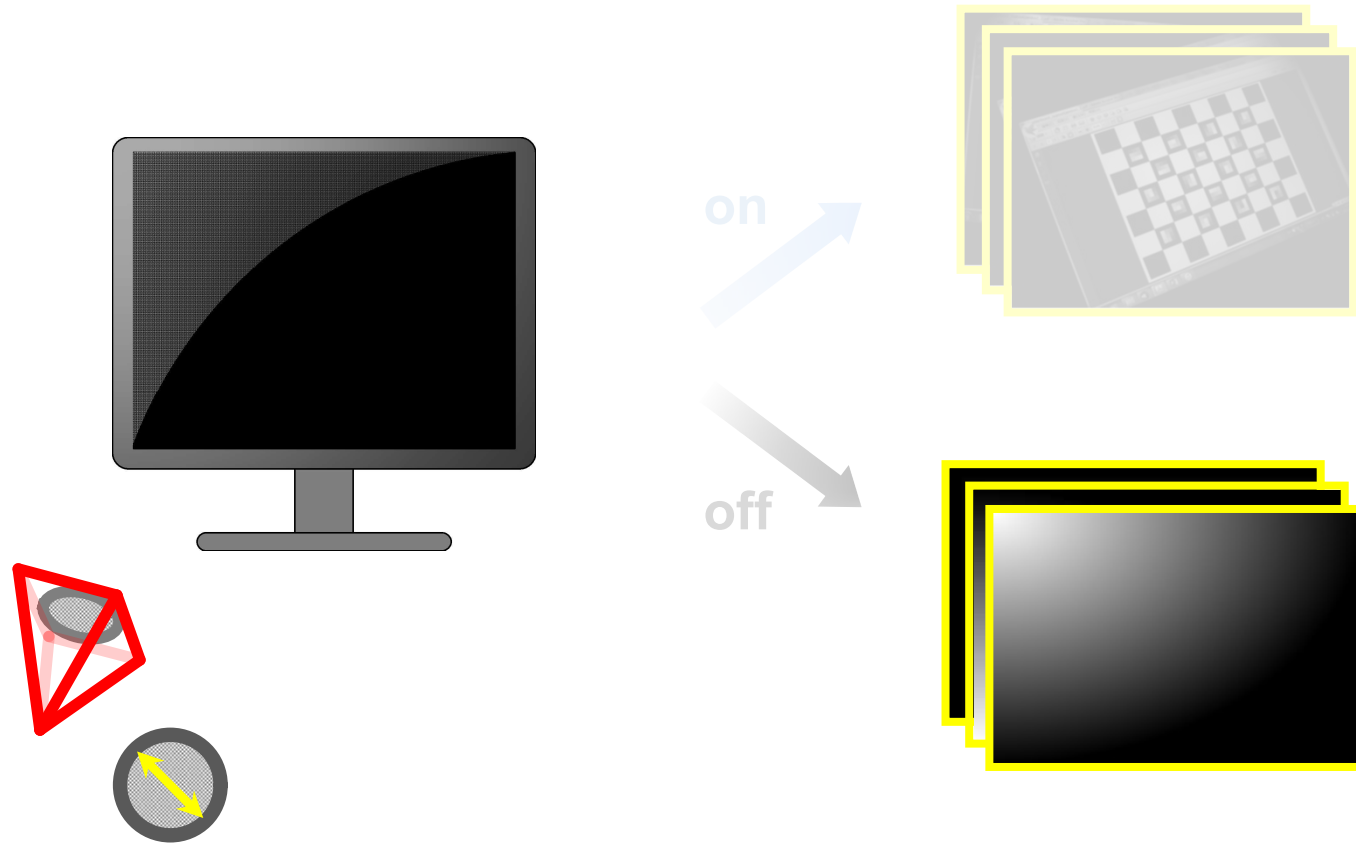
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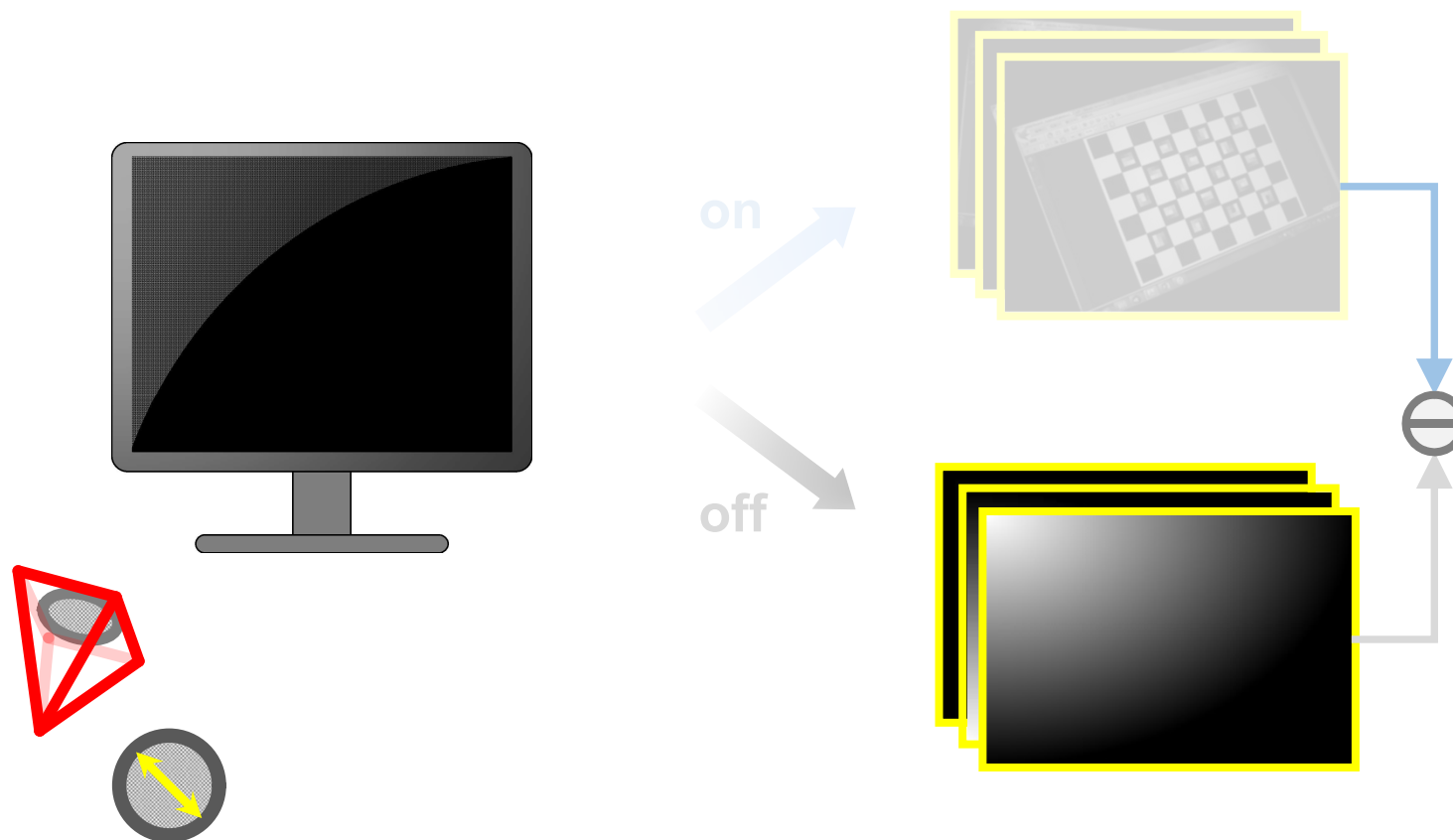
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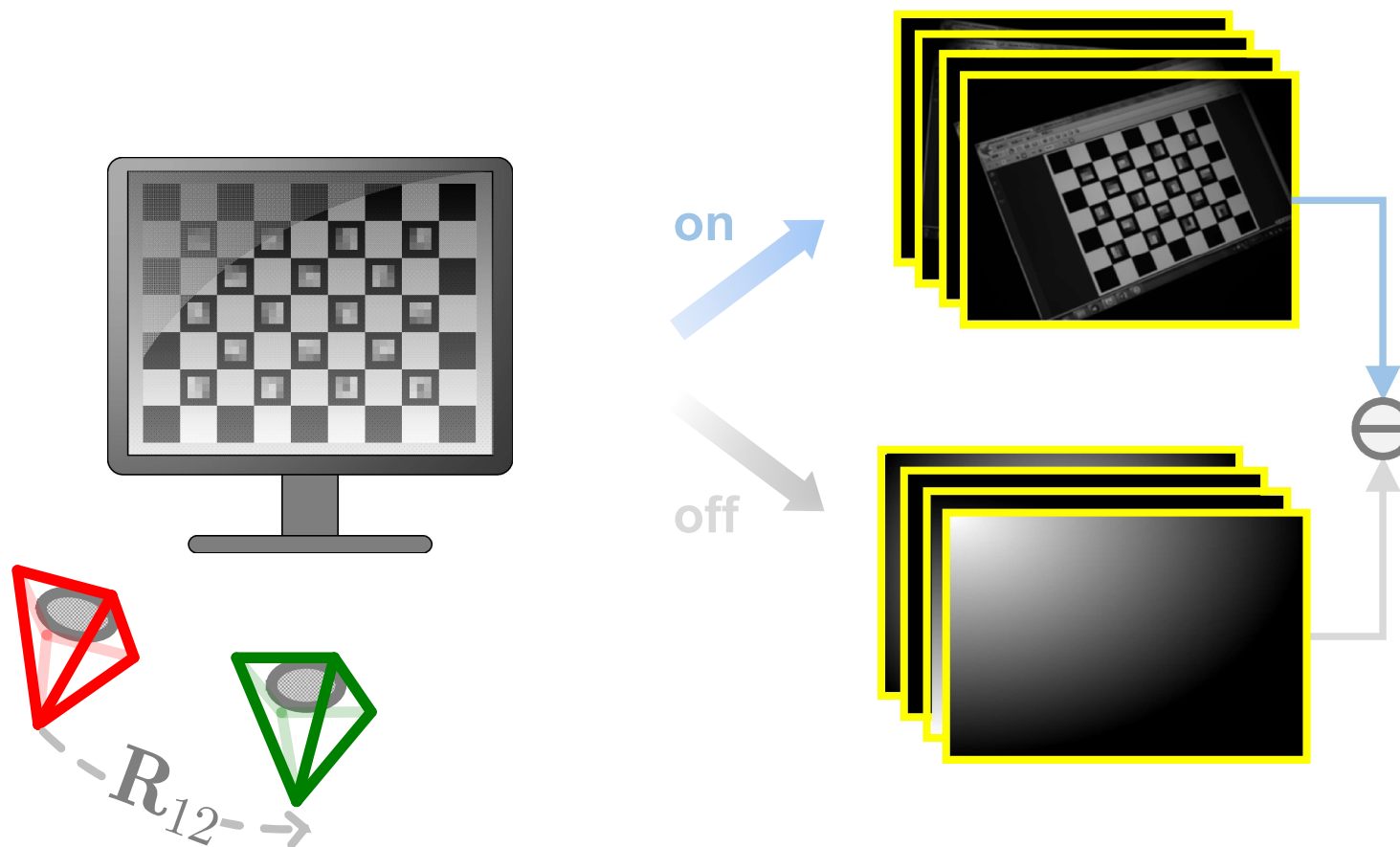
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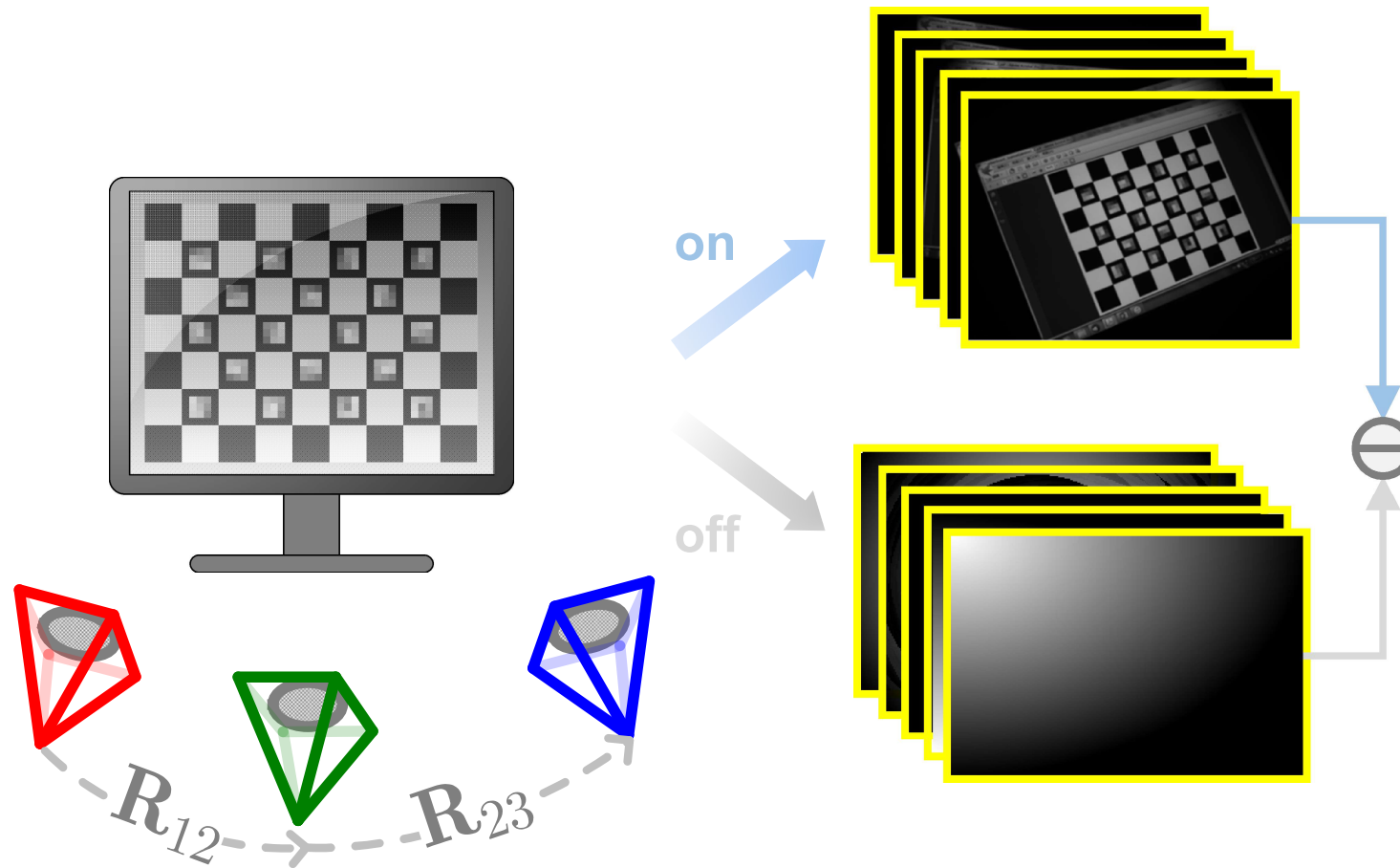
Method

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Method

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Method

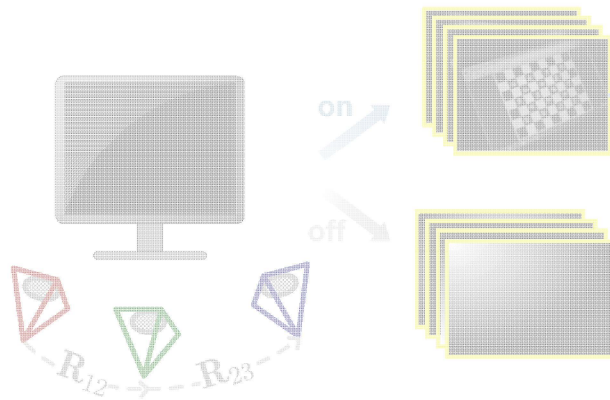
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$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

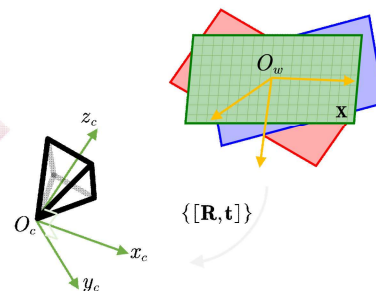
? ✓ ? ? ? ?

Overview

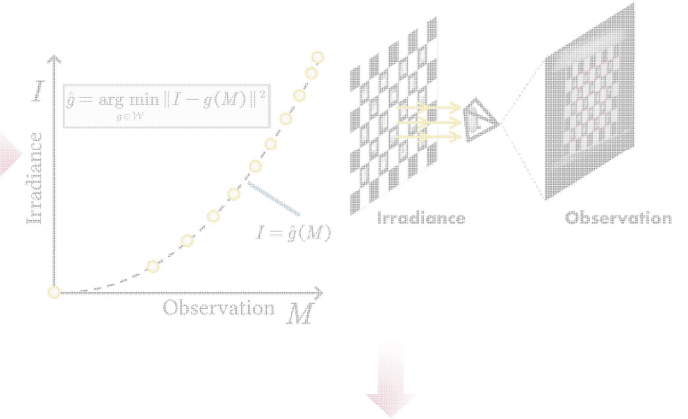
Step 1. Capture images



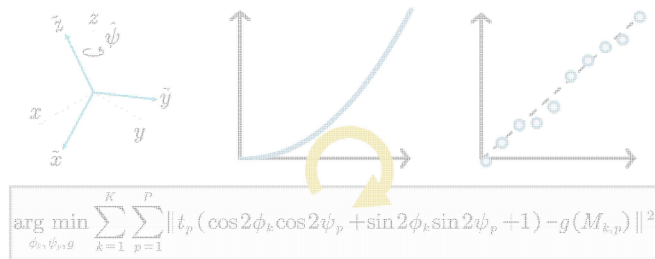
Step 2. Calibrate geometry



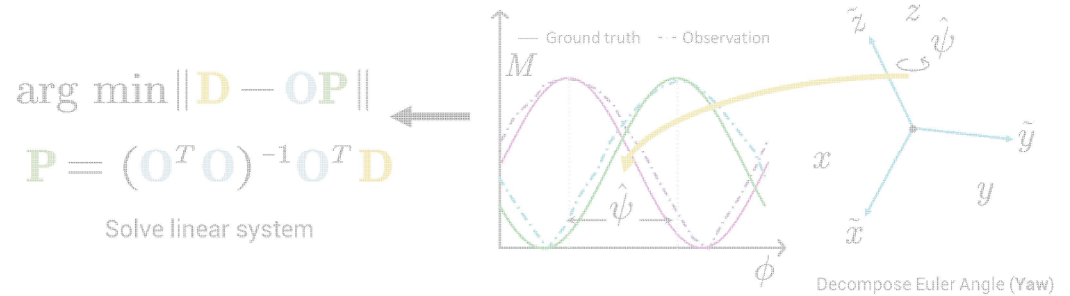
Step 3. Calibrate radiometry



Step 5. Bundle adjustment

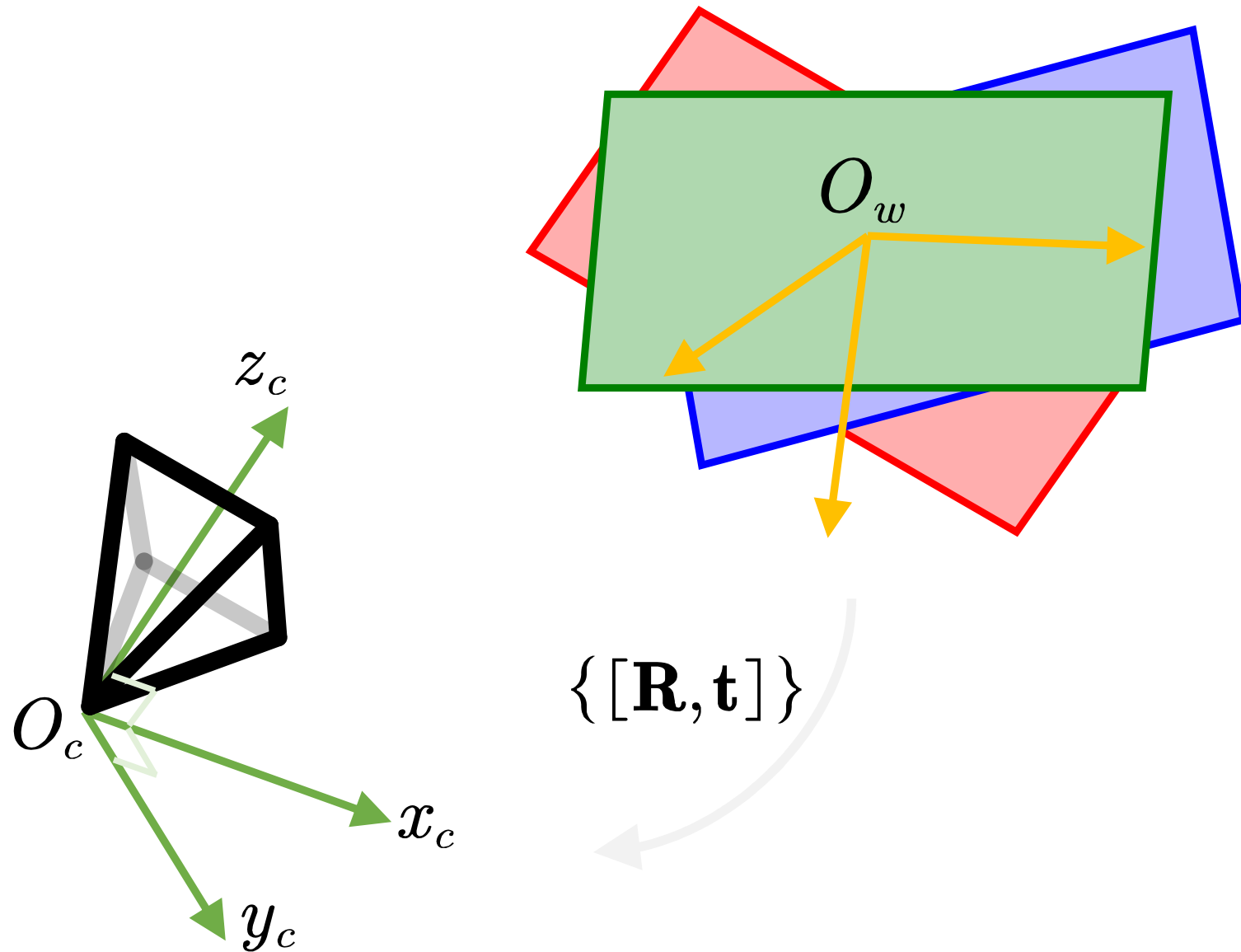


Step 4. Calibrate polarimetry



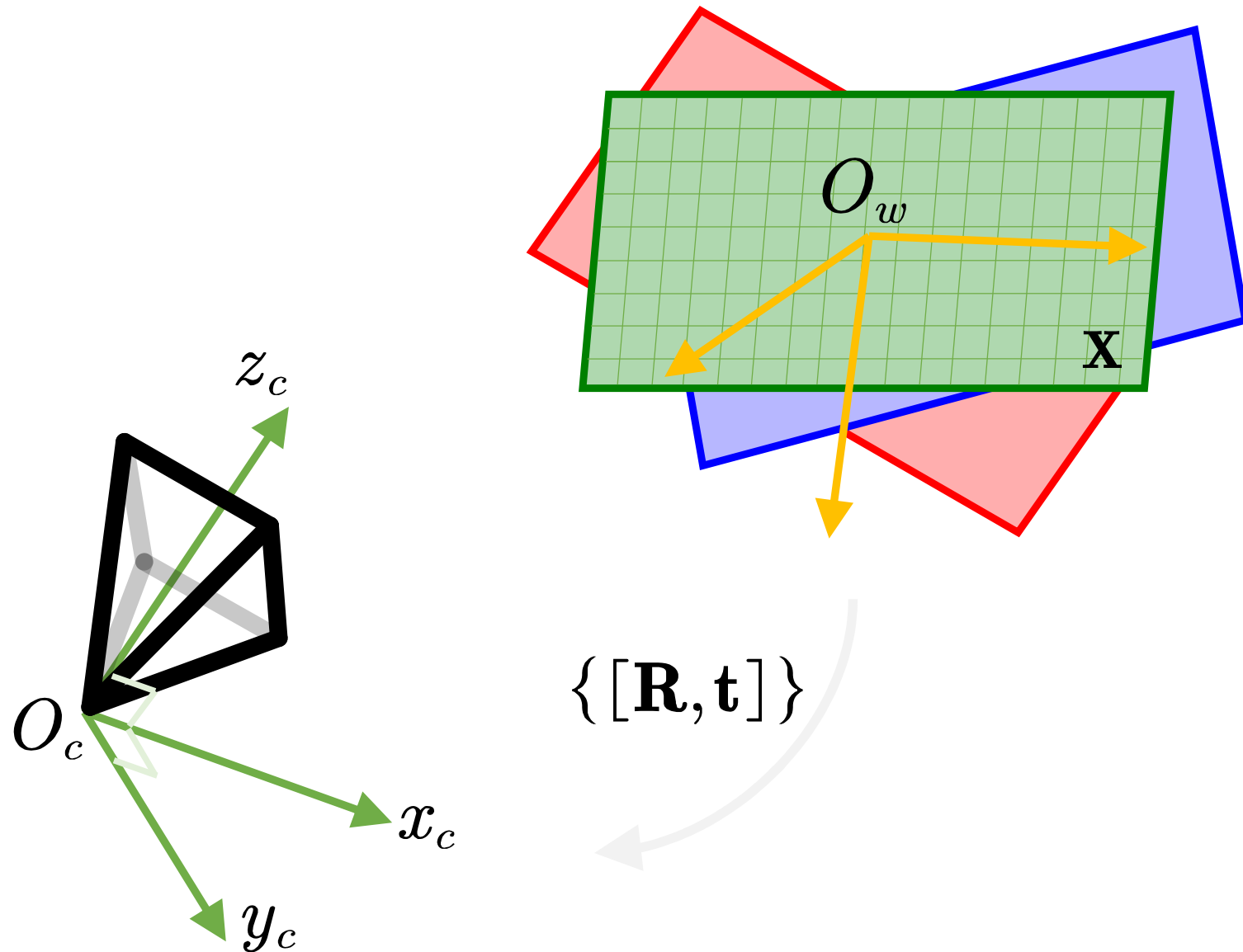
Method – Known CRF

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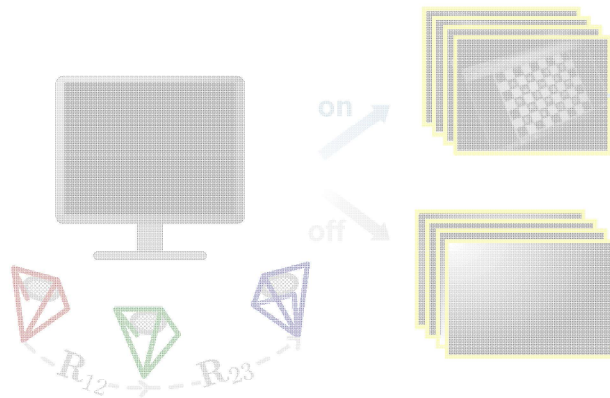
Method – Known CRF

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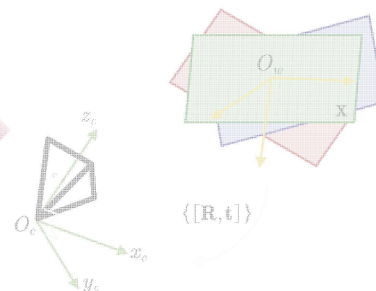


Overview

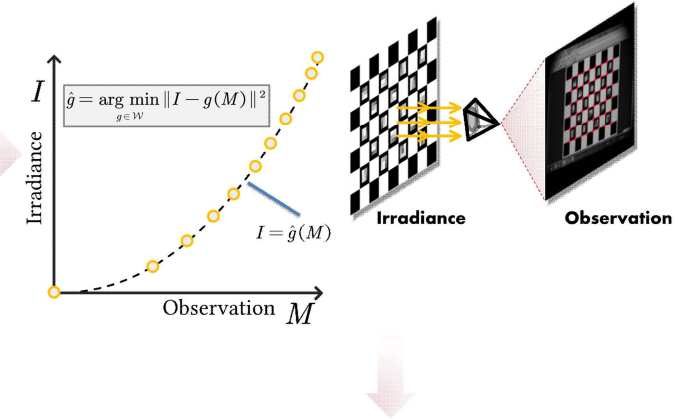
Step 1. Capture images



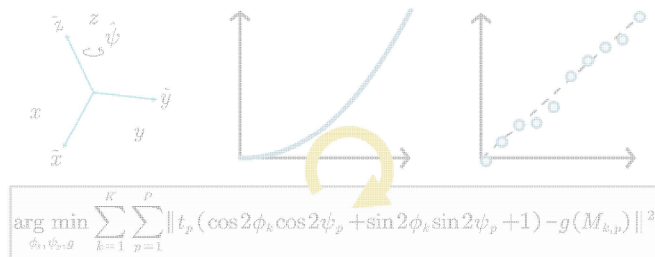
Step 2. Calibrate geometry



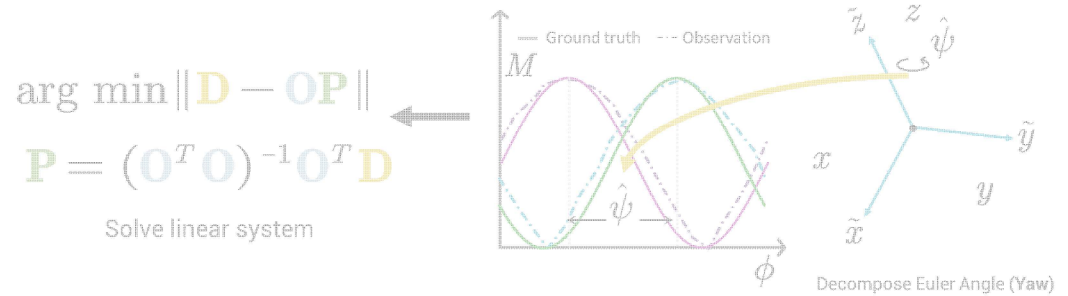
Step 3. Calibrate radiometry



Step 5. Bundle adjustment

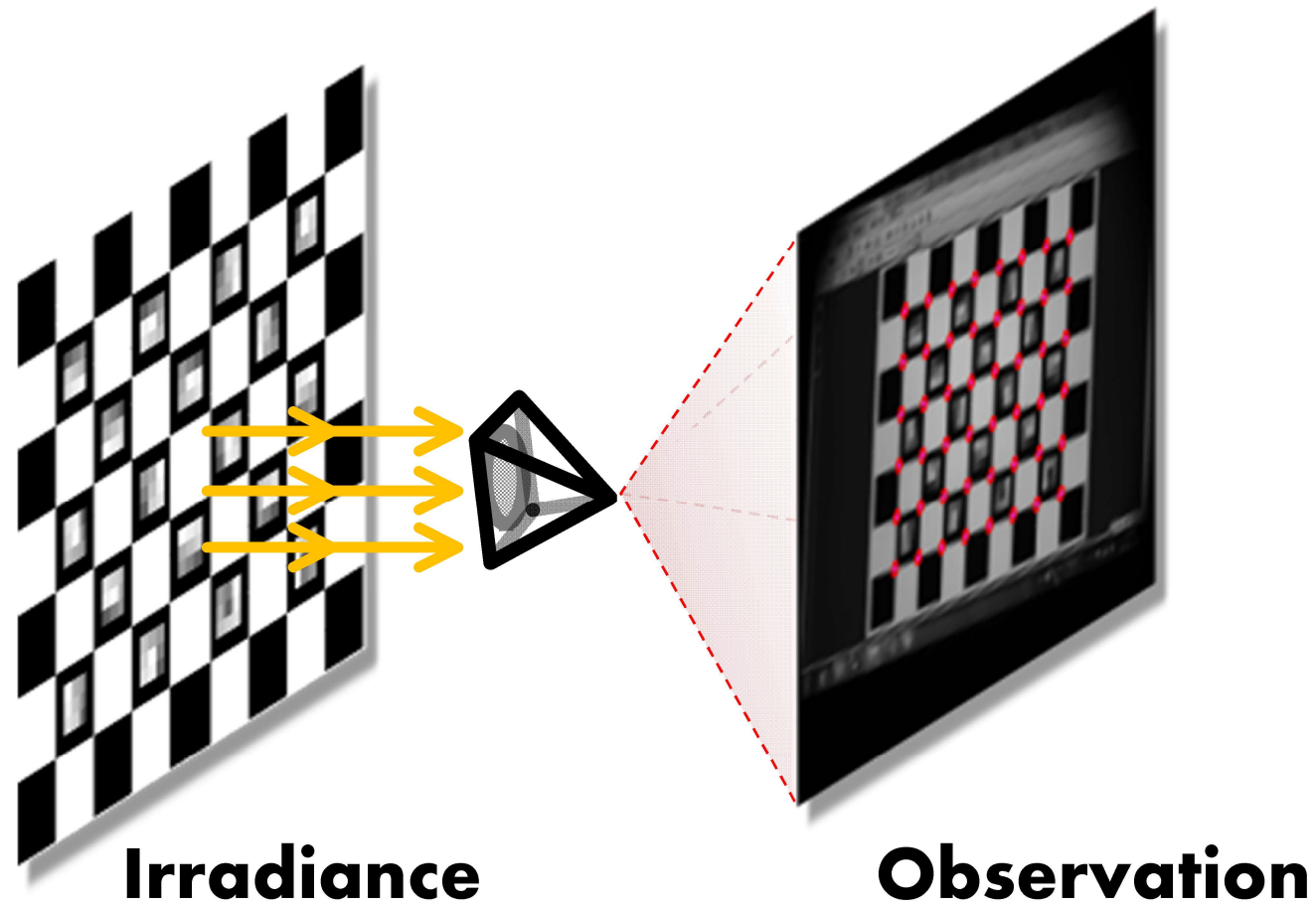


Step 4. Calibrate polarimetry



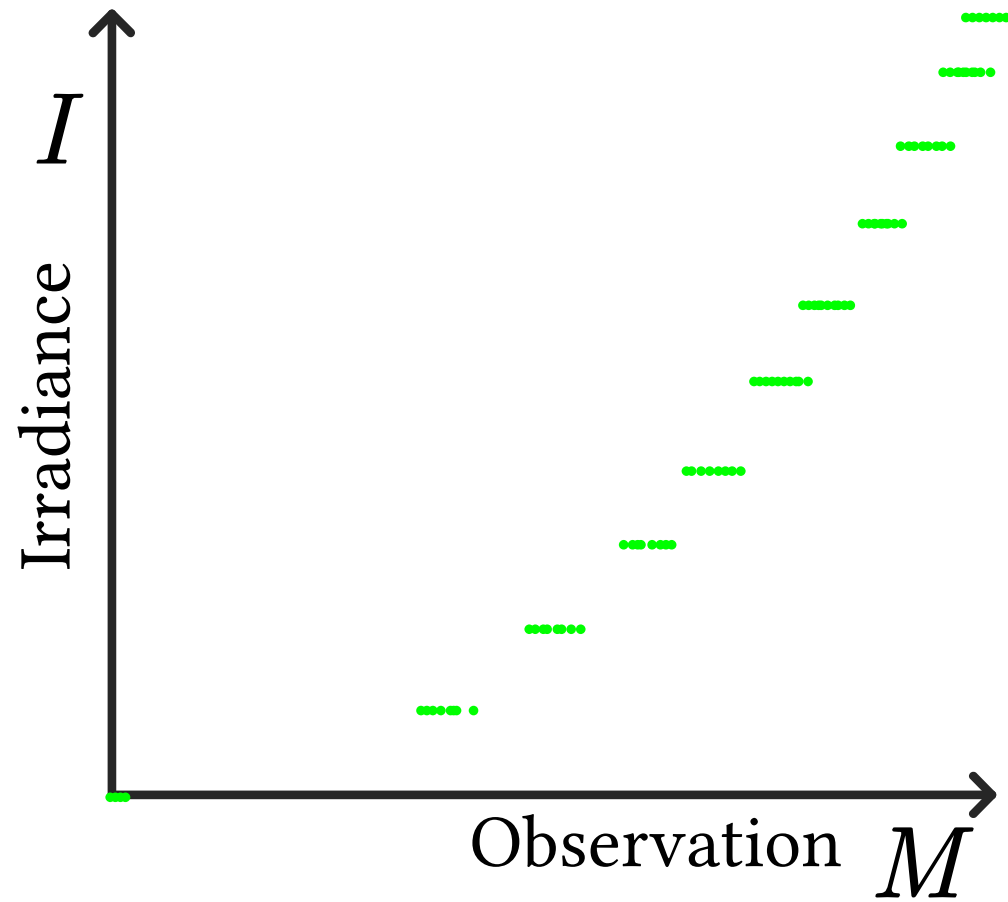
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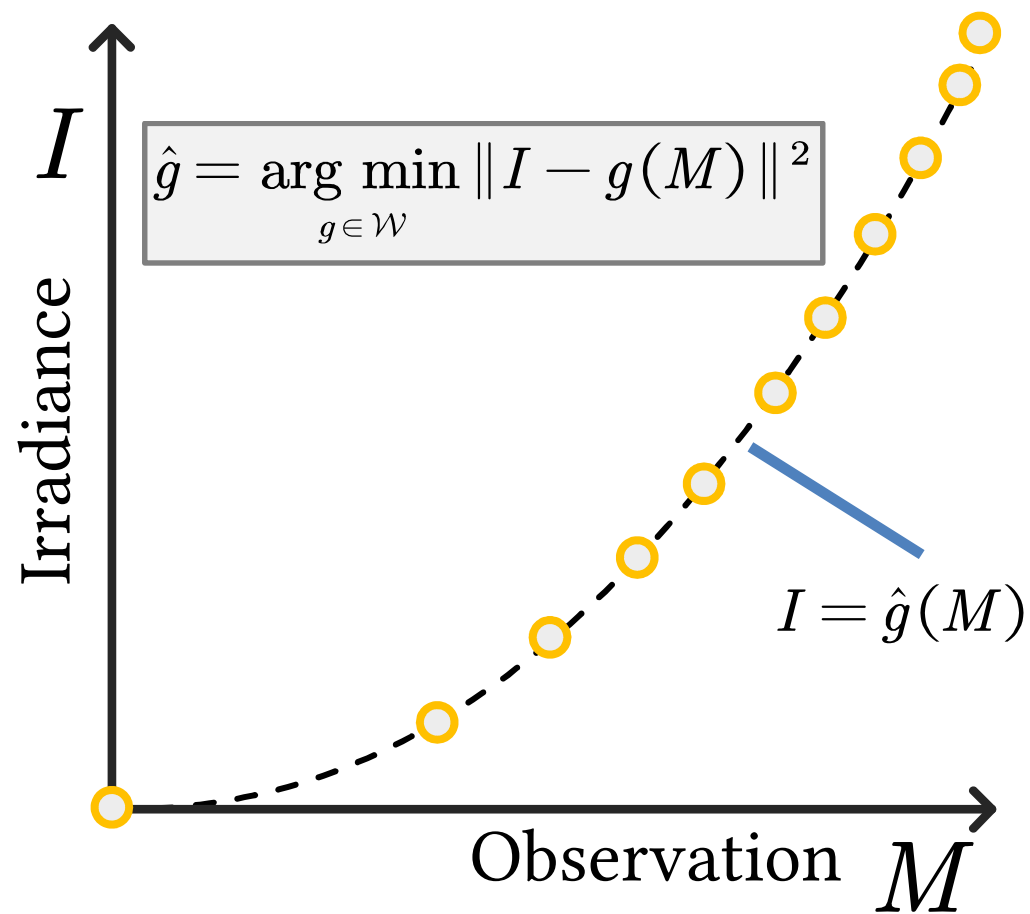
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Method

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Method

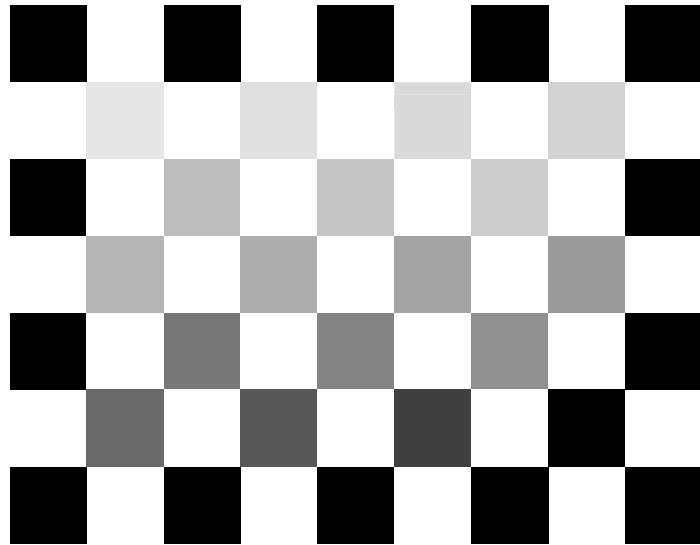
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$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

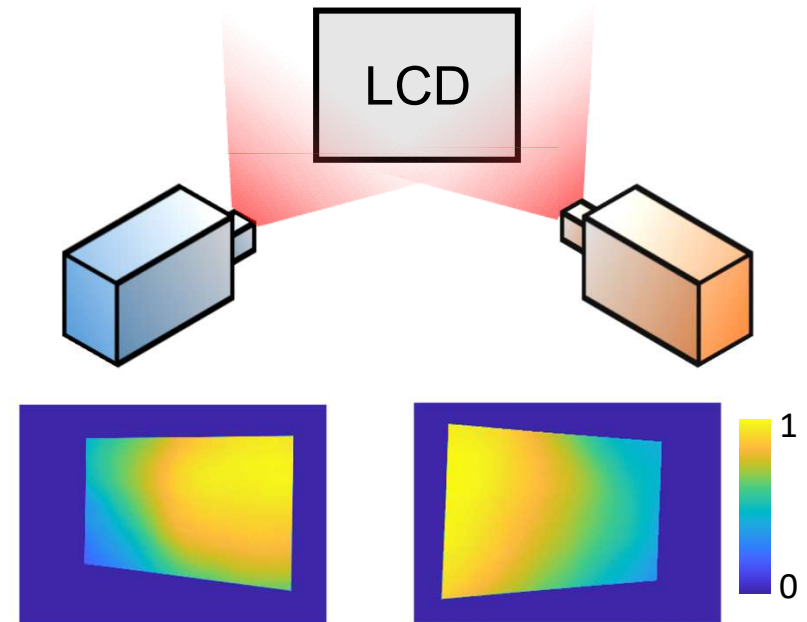
✓ ✓ ? ? ? ?

Method

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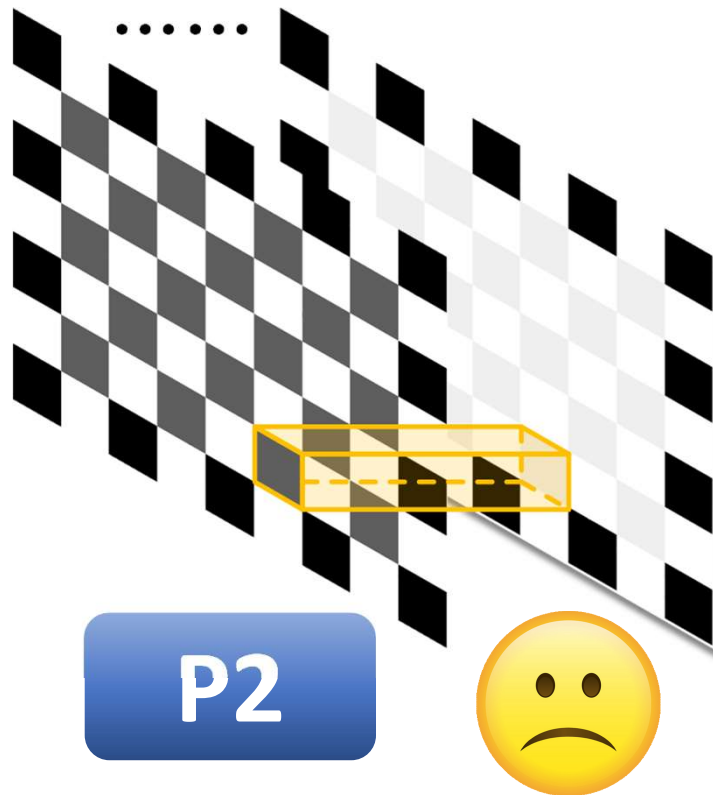
P1



Spatial inconsistency

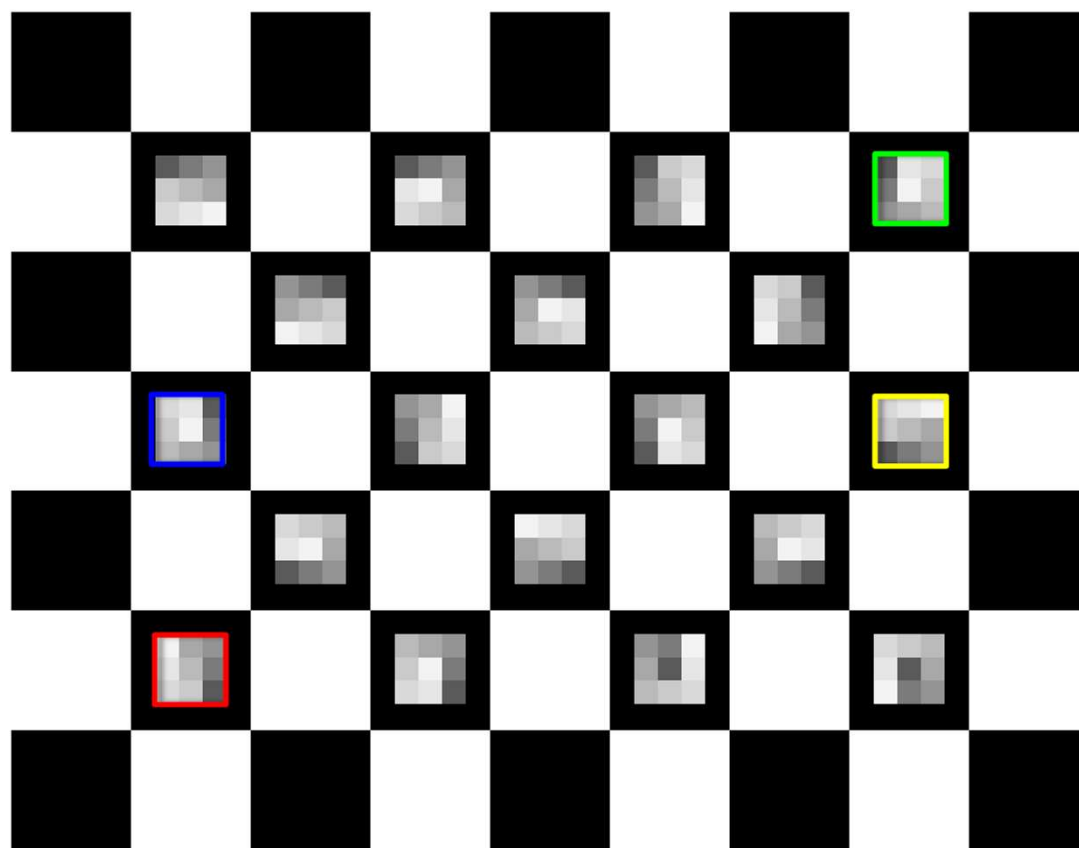
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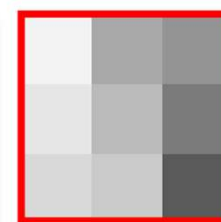
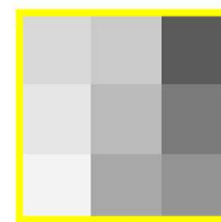
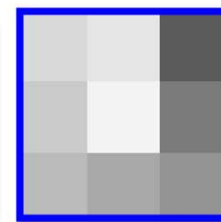
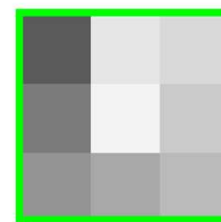


Method

54



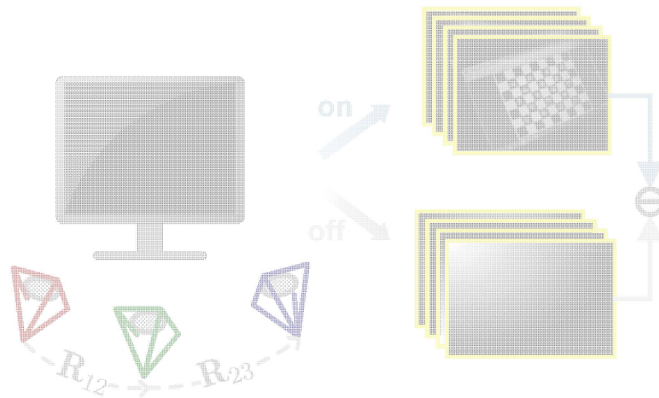
P3 (Ours)



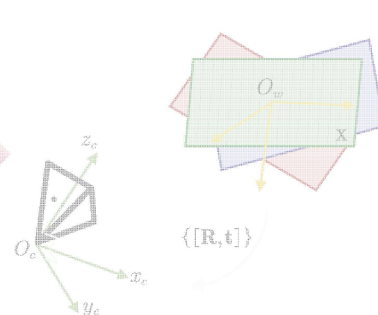
$$I_t = 255 \times [0.1, 0.2, \dots, 0.9]^{1/\gamma}$$

Overview

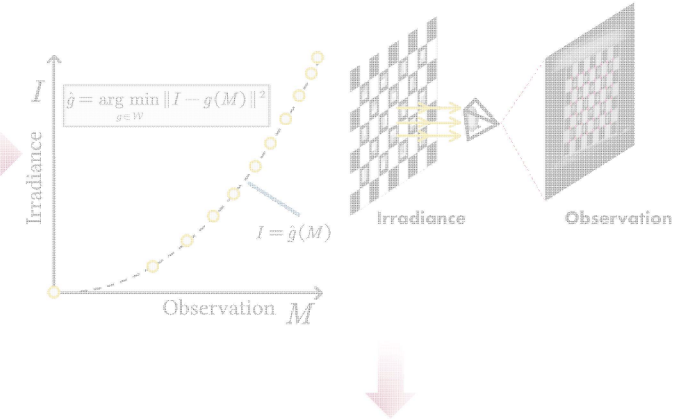
Step 1. Capture images



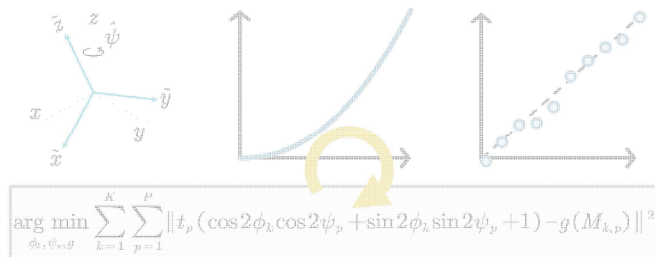
Step 2. Calibrate geometry



Step 3. Calibrate radiometry



Step 5. Bundle adjustment

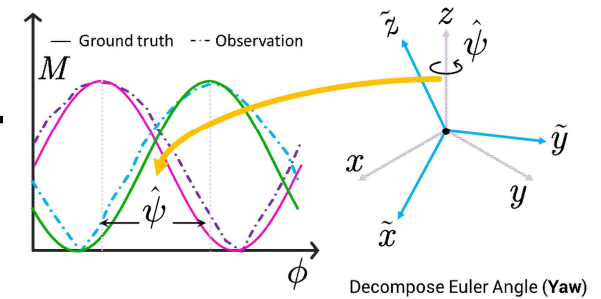


Step 4. Calibrate polarimetry

$$\arg \min \| \mathbf{D} - \mathbf{O} \mathbf{P} \|$$

$$\mathbf{P} = (\mathbf{O}^T \mathbf{O})^{-1} \mathbf{O}^T \mathbf{D}$$

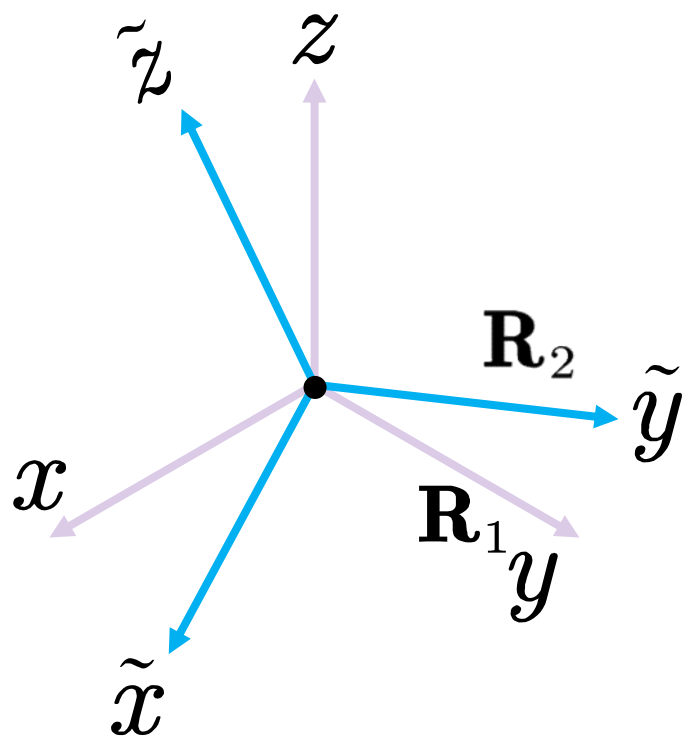
Solve linear system



Decompose Euler Angle (Yaw)

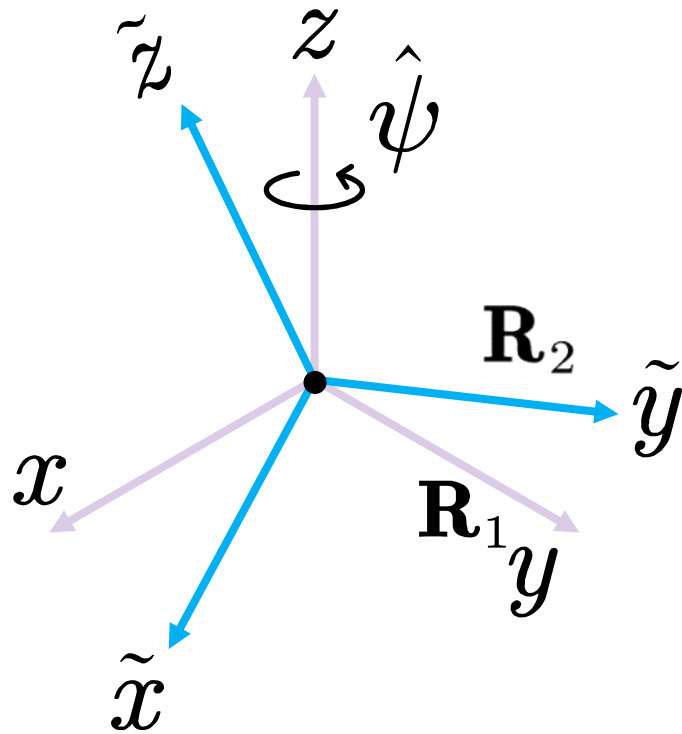
Method

56



Method

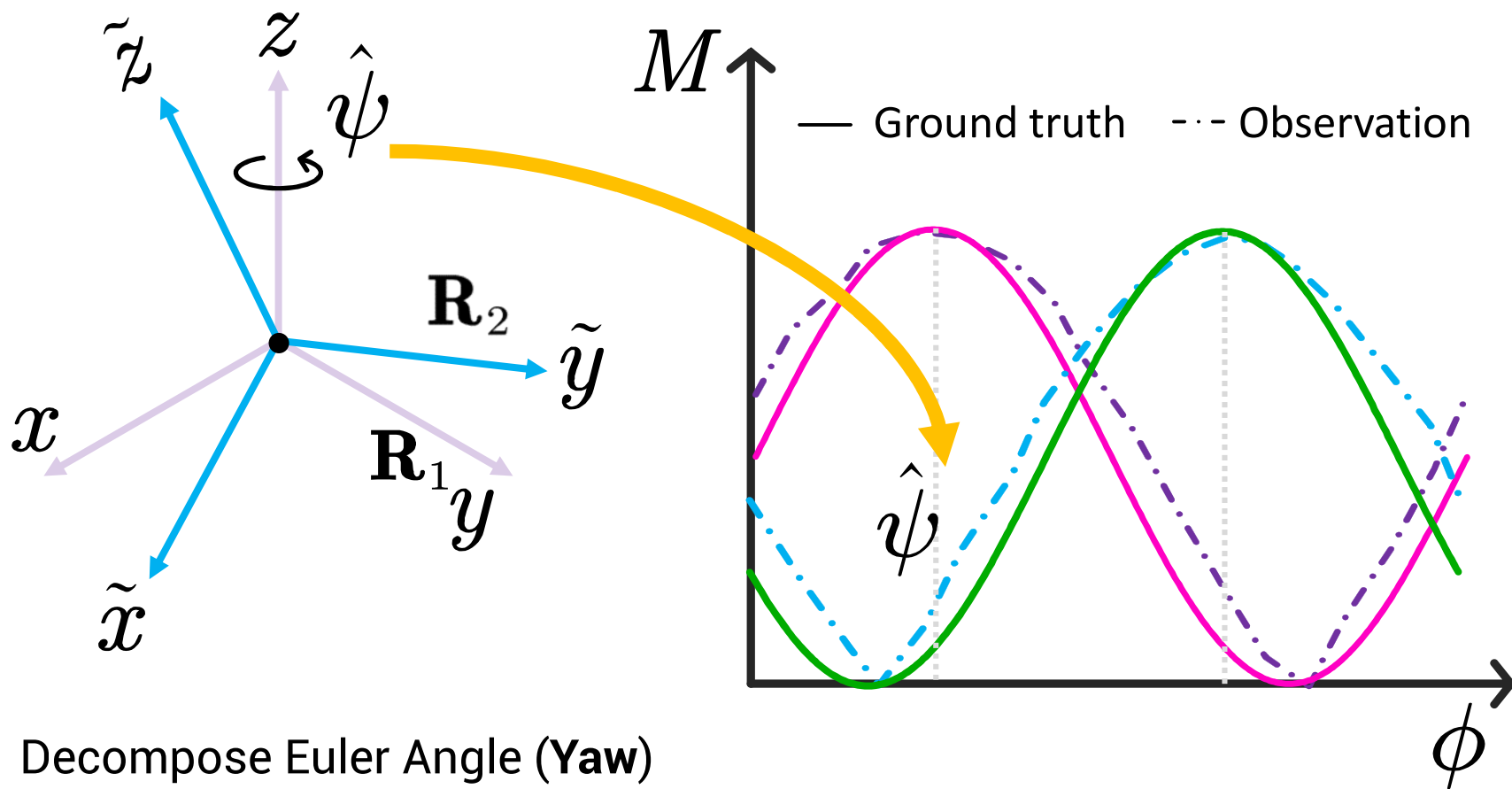
57



Decompose Euler Angle (Yaw)

Method

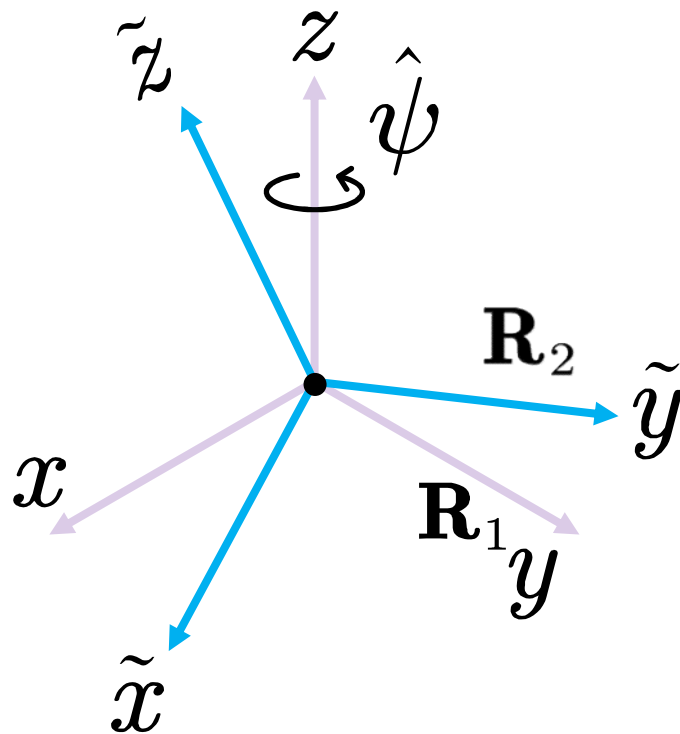
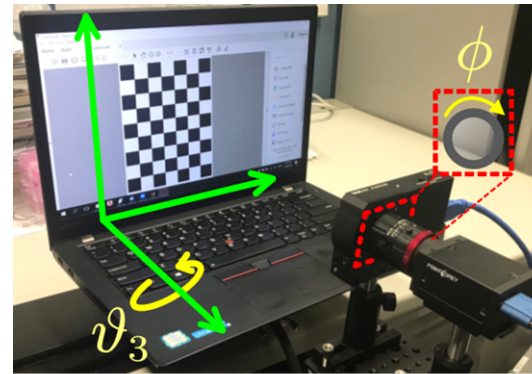
58



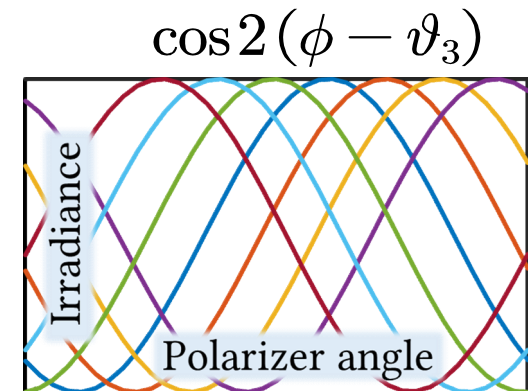
Method

59

Recall: in-plane rotation



Decompose Euler Angle (Yaw)



Method

60

$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

✓ ✓ ? ? ? ✓

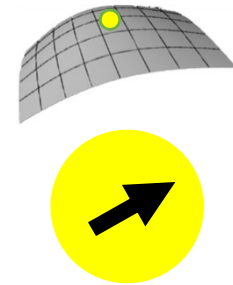
Method

61

$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

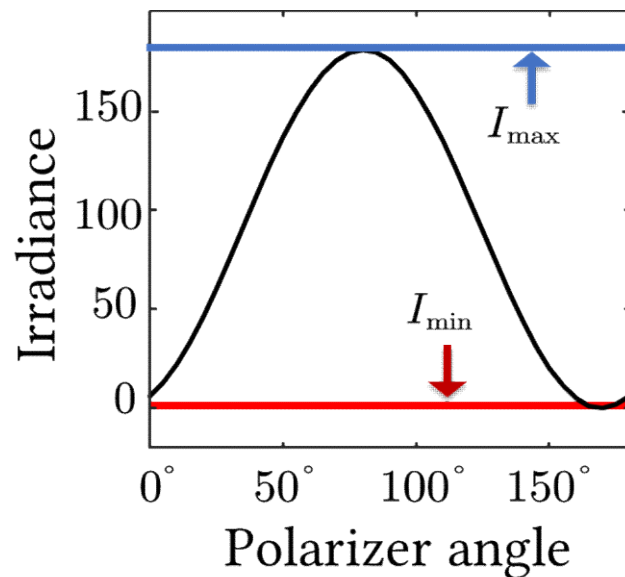
where

$$t_p = (I_{\max}(p) + I_{\min}(p))/2$$
$$a_p = (I_{\max}(p) - I_{\min}(p))/2$$



Recall

$$I_{\max} \gg I_{\min}$$



$$\text{let } t_p = a_p = I_{\max}(p)/2$$

$$\hat{g}(M_{k,p}) = t_p + \cancel{a_p} \cos 2(\phi_k - \hat{\psi}_p)$$

Method

62

$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

✓ ✓ ? ? ✓

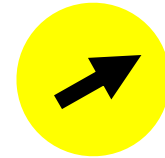
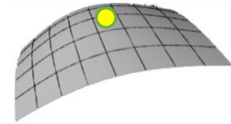
Method

63

$$\hat{g}(M_{k,p}) = t_p + t_p \cos 2(\phi_k - \hat{\psi}_p)$$

$$\hat{g}(M_{k,p}) = t_p (1 + \overset{\alpha_p}{\cos 2\psi_k} \cos 2\phi_k + \overset{\beta_p}{\sin 2\psi_k} \sin 2\phi_k)$$

✓ ✓ ? ✓ ✓



Method

64

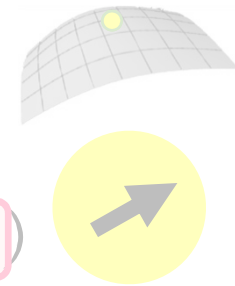
$$\hat{g}(M_{k,p}) = t_p + t_p \cos 2(\phi_k - \hat{\psi}_p)$$

$$\hat{g}(M_{k,p}) = t_p (1 + \overset{\alpha_p}{\cos 2\psi_k} \cos 2\phi_k + \overset{\beta_p}{\sin 2\psi_k} \sin 2\phi_k)$$



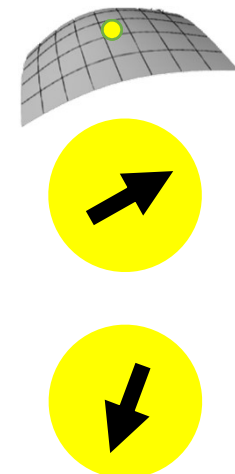






$$\hat{g}(M_{k,p}) = t_p (1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k)$$

$$\hat{g}(M_{1,p}) = t_p (1 + \alpha_p \cos 2\phi_1 + \beta_p \sin 2\phi_1)$$



Method

65

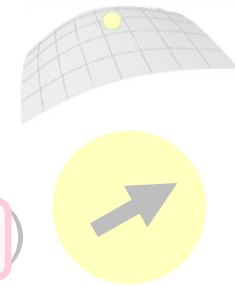
$$\hat{g}(M_{k,p}) = t_p + t_p \cos 2(\phi_k - \hat{\psi}_p)$$

$$\hat{g}(M_{k,p}) = t_p (1 + \overset{\alpha_p}{\cos 2\psi_k} \cos 2\phi_k + \overset{\beta_p}{\sin 2\psi_k} \sin 2\phi_k)$$



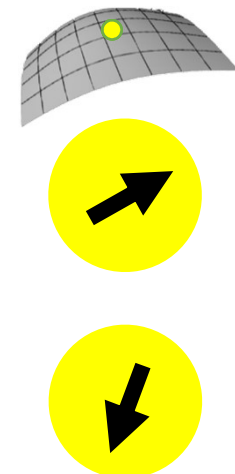






$$\frac{\hat{g}(M_{k,p})}{\hat{g}(M_{1,p})} = \frac{1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k}{1 + \alpha_p \cos 2\phi_1 + \beta_p \sin 2\phi_1}$$

where $\hat{g}(M_{1,p}) \neq 0$ $\phi_1 \neq \hat{\psi}_p \pm \pi/2$



Method

66

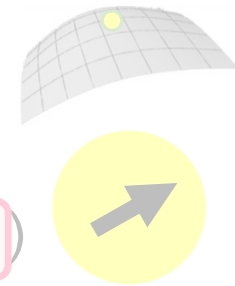
$$\hat{g}(M_{k,p}) = t_p + t_p \cos 2(\phi_k - \hat{\psi}_p)$$

$$\hat{g}(M_{k,p}) = t_p (1 + \overset{\alpha_p}{\cos 2\psi_k} \cos 2\phi_k + \overset{\beta_p}{\sin 2\psi_k} \sin 2\phi_k)$$



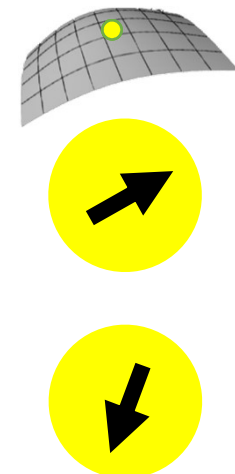






$$\frac{\hat{g}(M_{k,p})}{\hat{g}(M_{1,p})} = \frac{1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k}{1 + \alpha_p \cos 2\phi_1 + \beta_p \sin 2\phi_1}$$



Method

67

$$\hat{g}(M_{k,p}) = t_p + t_p \cos 2(\phi_k - \hat{\psi}_p)$$

$$\hat{g}(M_{k,p}) = t_p (1 + \overset{\alpha_p}{\cos 2\psi_k} \cos 2\phi_k + \overset{\beta_p}{\sin 2\psi_k} \sin 2\phi_k)$$

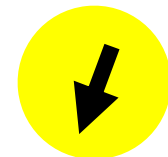
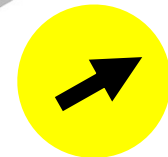
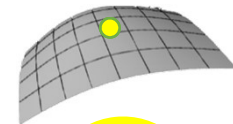
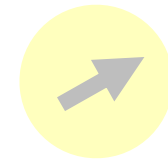
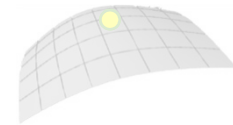
Annotations: Green checkmarks under $\cos 2\psi_k$ and $\sin 2\psi_k$; a blue question mark under $\cos 2\phi_k$; a yellow circle with a right-pointing arrow on the right.

$$\frac{\hat{g}(M_{k,p})}{\hat{g}(M_{1,p})} = \frac{1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k}{1 + \alpha_p \cos 2\phi_1 + \beta_p \sin 2\phi_1}$$

Annotations: Red and blue arrows pointing from the numerator and denominator terms to the fraction bar.

$$I_{k,p} - I_{1,p} = I_{1,p} \alpha_p \cos 2\phi_k + I_{1,p} \beta_p \sin 2\phi_k \\ - I_{k,p} \alpha_p \cos 2\phi_1 + I_{k,p} \beta_p \sin 2\phi_1$$

where $I_{k,p} = \hat{g}(M_{k,p})$



Method

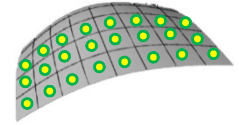
68

$$\hat{g}(M_{k,p}) = t_p + a_p \cos 2(\phi_k - \hat{\psi}_p)$$

✓ ✓ ? ✓

Method

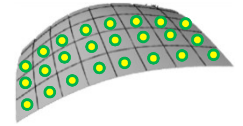
69



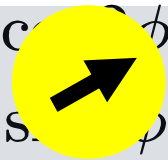
$$\begin{bmatrix} \hat{I}_{1,1} - \hat{I}_{2,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{2,P} \\ \vdots \\ \hat{I}_{1,1} - \hat{I}_{K,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{K,P} \end{bmatrix} = \begin{bmatrix} \begin{matrix} \alpha_1 \hat{I}_{2,1} & \beta_1 \hat{I}_{2,1} \\ \alpha_2 \hat{I}_{2,2} & \beta_2 \hat{I}_{2,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{2,P} & \beta_P \hat{I}_{2,P} \end{matrix} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \mathbf{0} & \cdots & \mathbf{0} \\ \begin{matrix} \alpha_1 \hat{I}_{3,1} & \beta_1 \hat{I}_{3,1} \\ \alpha_2 \hat{I}_{3,2} & \beta_2 \hat{I}_{3,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{3,P} & \beta_P \hat{I}_{3,P} \end{matrix} & \mathbf{0} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \cdots & \mathbf{0} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \begin{matrix} \alpha_1 \hat{I}_{K,1} & \beta_1 \hat{I}_{K,1} \\ \alpha_2 \hat{I}_{K,2} & \beta_2 \hat{I}_{K,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{K,P} & \beta_P \hat{I}_{K,P} \end{matrix} & \mathbf{0} & \mathbf{0} & \cdots & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} \end{bmatrix} \begin{bmatrix} \cos 2\phi_1 \\ \sin 2\phi_1 \\ \vdots \\ \cos 2\phi_K \\ \sin 2\phi_K \end{bmatrix}$$

Method

70

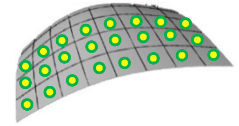


$$\begin{bmatrix} \hat{I}_{1,1} - \hat{I}_{2,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{2,P} \\ \vdots \\ \hat{I}_{1,1} - \hat{I}_{K,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{K,P} \end{bmatrix} = \begin{bmatrix} \begin{matrix} \alpha_1 \hat{I}_{2,1} & \beta_1 \hat{I}_{2,1} \\ \alpha_2 \hat{I}_{2,2} & \beta_2 \hat{I}_{2,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{2,P} & \beta_P \hat{I}_{2,P} \end{matrix} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \mathbf{0} & \cdots & \mathbf{0} \\ \begin{matrix} \alpha_1 \hat{I}_{3,1} & \beta_1 \hat{I}_{3,1} \\ \alpha_2 \hat{I}_{3,2} & \beta_2 \hat{I}_{3,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{3,P} & \beta_P \hat{I}_{3,P} \end{matrix} & \mathbf{0} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \cdots & \mathbf{0} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \begin{matrix} \alpha_1 \hat{I}_{K,1} & \beta_1 \hat{I}_{K,1} \\ \alpha_2 \hat{I}_{K,2} & \beta_2 \hat{I}_{K,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{K,P} & \beta_P \hat{I}_{K,P} \end{matrix} & \mathbf{0} & \mathbf{0} & \cdots & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} \end{bmatrix} \begin{bmatrix} \text{Coeff } \phi_1 \\ \text{Slope } \rho_1 \\ \vdots \\ \text{Coeff } \phi_K \\ \text{Slope } \rho_K \end{bmatrix}$$



Method

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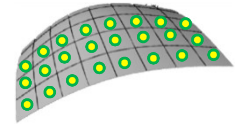


$$\begin{bmatrix} \hat{I}_{1,1} - \hat{I}_{2,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{2,P} \\ \vdots \\ \hat{I}_{1,1} - \hat{I}_{K,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{K,P} \end{bmatrix} = \begin{bmatrix} \begin{matrix} \alpha_1 \hat{I}_{2,1} & \beta_1 \hat{I}_{2,1} \\ \alpha_2 \hat{I}_{2,2} & \beta_2 \hat{I}_{2,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{2,P} & \beta_P \hat{I}_{2,P} \end{matrix} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \begin{matrix} 0 \\ 0 \\ \vdots \\ 0 \end{matrix} & \dots & \begin{matrix} 0 \\ 0 \\ \vdots \\ 0 \end{matrix} \\ \begin{matrix} \alpha_1 \hat{I}_{3,1} & \beta_1 \hat{I}_{3,1} \\ \alpha_2 \hat{I}_{3,2} & \beta_2 \hat{I}_{3,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{3,P} & \beta_P \hat{I}_{3,P} \end{matrix} & \begin{matrix} 0 \\ 0 \\ \vdots \\ 0 \end{matrix} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \dots & \begin{matrix} 0 \\ 0 \\ \vdots \\ 0 \end{matrix} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \begin{matrix} \alpha_1 \hat{I}_{K,1} & \beta_1 \hat{I}_{K,1} \\ \alpha_2 \hat{I}_{K,2} & \beta_2 \hat{I}_{K,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{K,P} & \beta_P \hat{I}_{K,P} \end{matrix} & \begin{matrix} 0 \\ 0 \\ \vdots \\ 0 \end{matrix} & \begin{matrix} 0 \\ 0 \\ \vdots \\ 0 \end{matrix} & \dots & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} \end{bmatrix} \begin{bmatrix} \cos 2\phi_1 \\ \sin 2\phi_1 \\ \vdots \\ \cos 2\phi_K \\ \sin 2\phi_K \end{bmatrix}$$

P

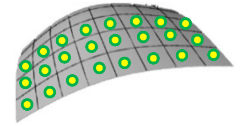
Method

72



$$\begin{bmatrix} \hat{I}_{1,1} - \hat{I}_{2,1} \\ \vdots \\ \hat{I}_{1,P} - \hat{I}_{K,P} \end{bmatrix} \mathbf{D} = \begin{bmatrix} \begin{matrix} \alpha_1 \hat{I}_{2,1} & \beta_1 \hat{I}_{2,1} \\ \alpha_2 \hat{I}_{2,2} & \beta_2 \hat{I}_{2,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{2,P} & \beta_P \hat{I}_{2,P} \end{matrix} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \mathbf{0} & \cdots & \mathbf{0} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \begin{matrix} \alpha_1 \hat{I}_{3,1} & \beta_1 \hat{I}_{3,1} \\ \alpha_2 \hat{I}_{3,2} & \beta_2 \hat{I}_{3,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{3,P} & \beta_P \hat{I}_{3,P} \end{matrix} & \mathbf{0} & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} & \cdots & \mathbf{0} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \begin{matrix} \alpha_1 \hat{I}_{K,1} & \beta_1 \hat{I}_{K,1} \\ \alpha_2 \hat{I}_{K,2} & \beta_2 \hat{I}_{K,2} \\ \vdots & \vdots \\ \alpha_P \hat{I}_{K,P} & \beta_P \hat{I}_{K,P} \end{matrix} & \mathbf{0} & \mathbf{0} & \cdots & \begin{matrix} -\alpha_1 \hat{I}_{1,1} & -\beta_1 \hat{I}_{1,1} \\ -\alpha_2 \hat{I}_{1,2} & -\beta_2 \hat{I}_{1,2} \\ \vdots & \vdots \\ -\alpha_P \hat{I}_{1,P} & -\beta_P \hat{I}_{1,P} \end{matrix} \end{bmatrix} \mathbf{P} \begin{bmatrix} \cos 2\phi_1 \\ \sin 2\phi_1 \\ \vdots \\ \cos 2\phi_K \\ \sin 2\phi_K \end{bmatrix}$$

$$\mathbf{D} = \mathbf{O} \mathbf{P}$$



$$\arg \min \|\mathbf{D} - \mathbf{O} \mathbf{P}\|$$

Solve linear system

$$\mathbf{P} = (\mathbf{O}^T \mathbf{O})^{-1} \mathbf{O}^T \mathbf{D}$$

Method

74

Radiometry



Geometry



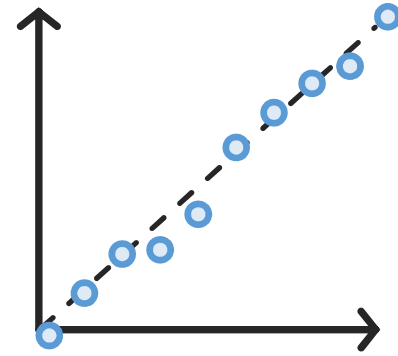
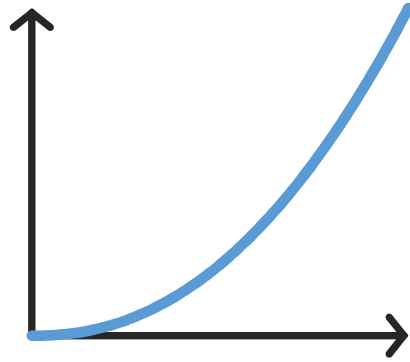
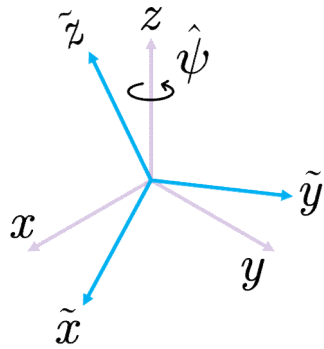
Polarimetry

$$\hat{g}(M_{k,p}) = t_p + a \cos 2(\phi_k - \hat{\psi}_p)$$



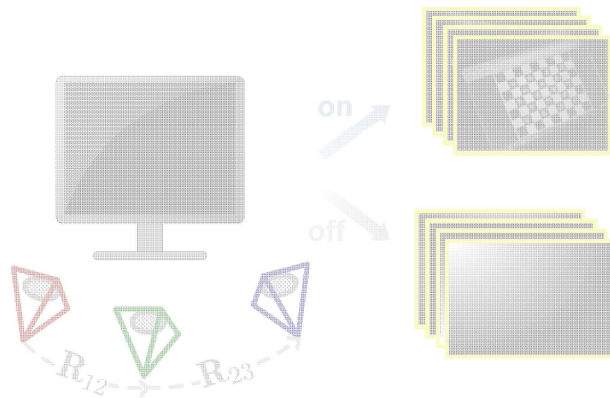
Method

75

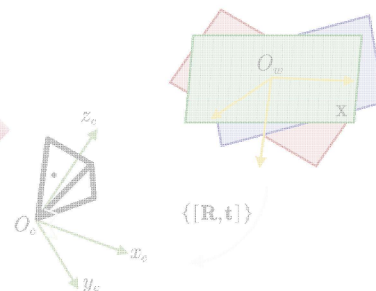


Overview

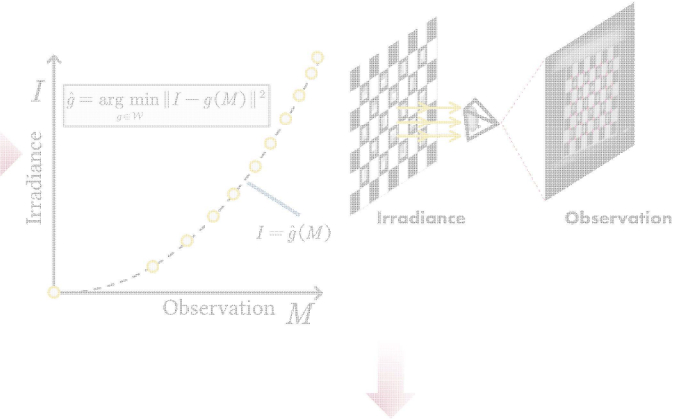
Step 1. Capture images



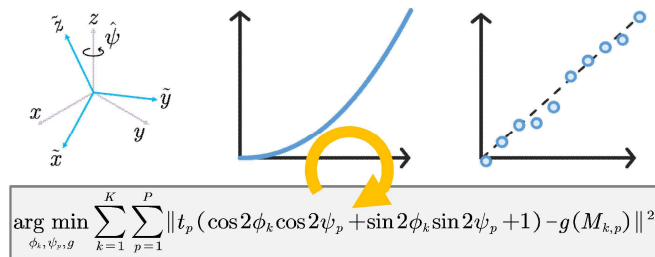
Step 2. Calibrate geometry



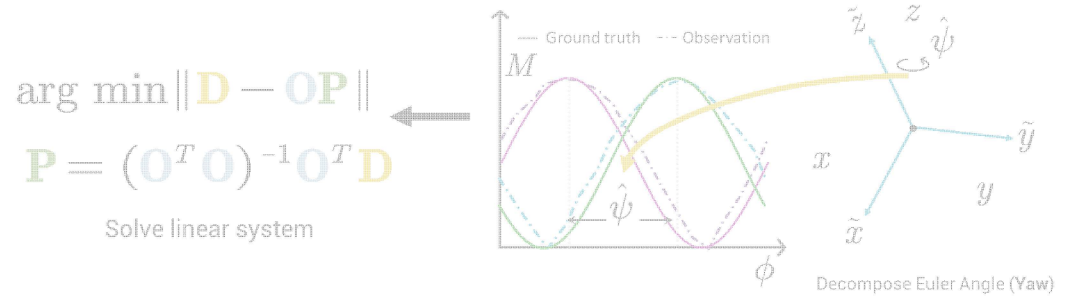
Step 3. Calibrate radiometry



Step 5. Bundle adjustment

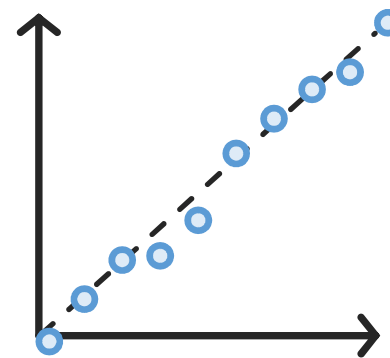
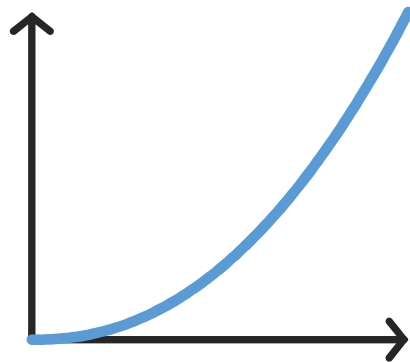
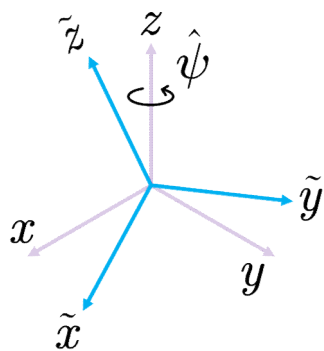


Step 4. Calibrate polarimetry



Method

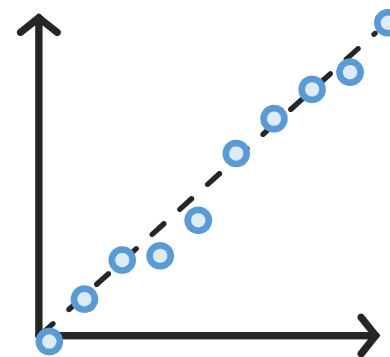
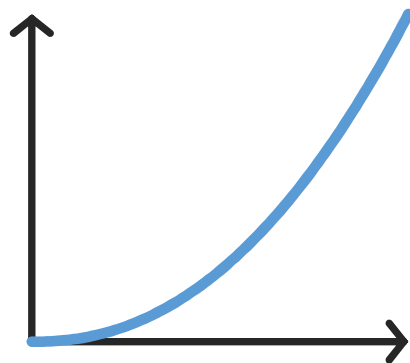
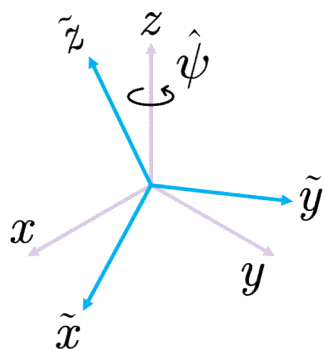
77



$$\arg \min_{\phi_k, \psi_p, g} \sum_{k=1}^K \sum_{p=1}^P \| t_p (\cos 2\phi_k \cos 2\psi_p + \sin 2\phi_k \sin 2\psi_p + 1) - g(M_{k,p}) \|^2$$

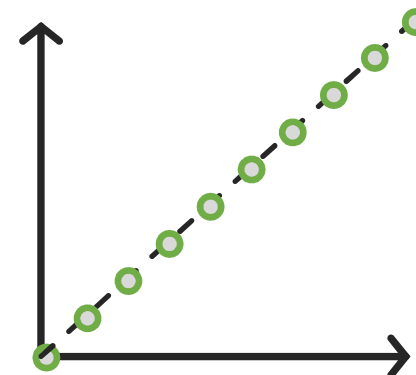
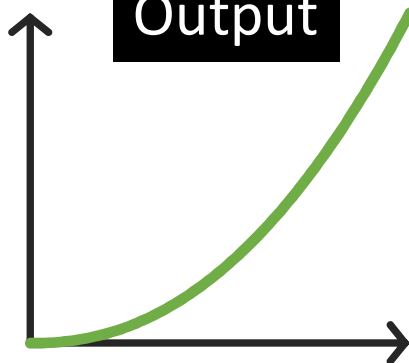
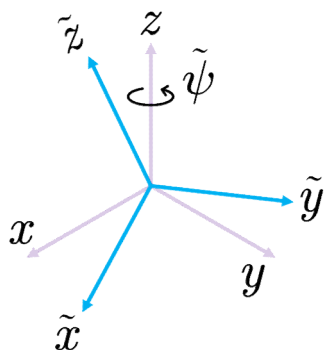
Method

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$$\arg \min_{\phi_k, \psi_p, g} \sum_{k=1}^K \sum_{p=1}^P \| t_p (\cos 2\phi_k \cos 2\psi_p + \sin 2\phi_k \sin 2\psi_p + 1) - g(M_{k,p}) \|^2$$

Output



$$\hat{g}(M_{k,p}) = t_p (1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k)$$

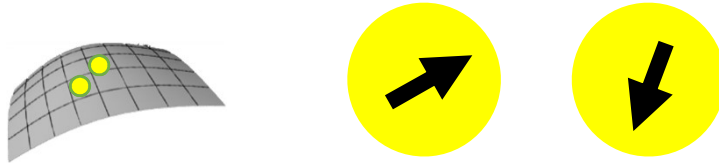
$$KP \text{ data} \quad \geq \quad P+K \text{ unknown}$$

Method

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$$\hat{g}(M_{k,p}) = t_p (1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k)$$

KP data $\geq$ *P+K unknown*



At least

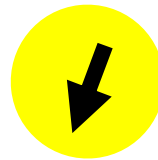
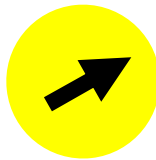
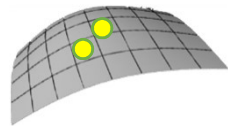
- 2 object points
- 2 polarizing channels

Method

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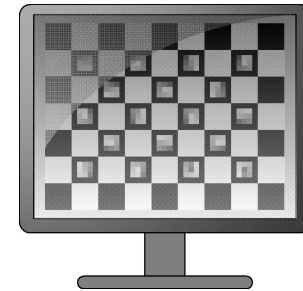
$$\hat{g}(M_{k,p}) = t_p (1 + \alpha_p \cos 2\phi_k + \beta_p \sin 2\phi_k)$$

KP data $\geq$ *P+K unknown*



At least

- 2 object points
- 2 polarizing channels



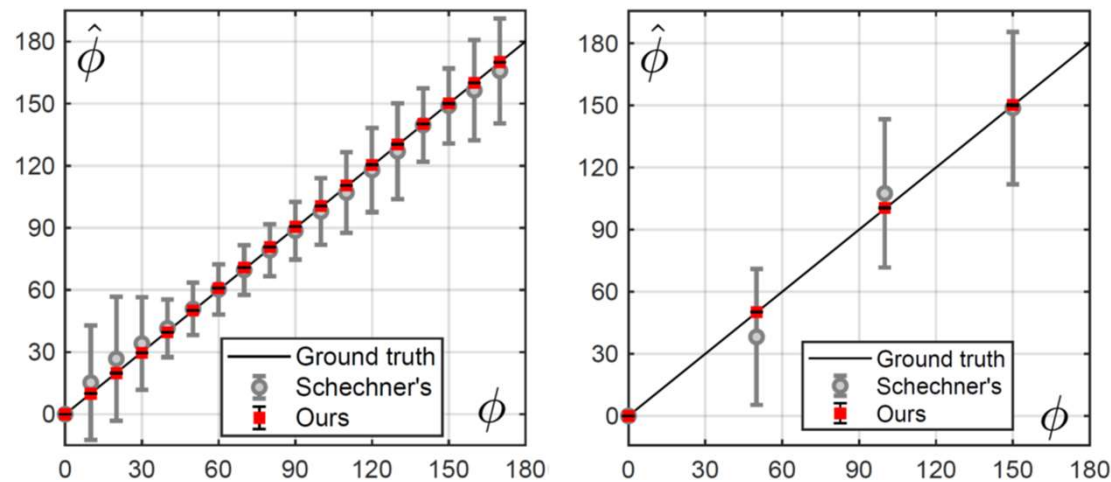
At least

- rotate once in the polarizer plane

Experiments – Simulation

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Known CRF

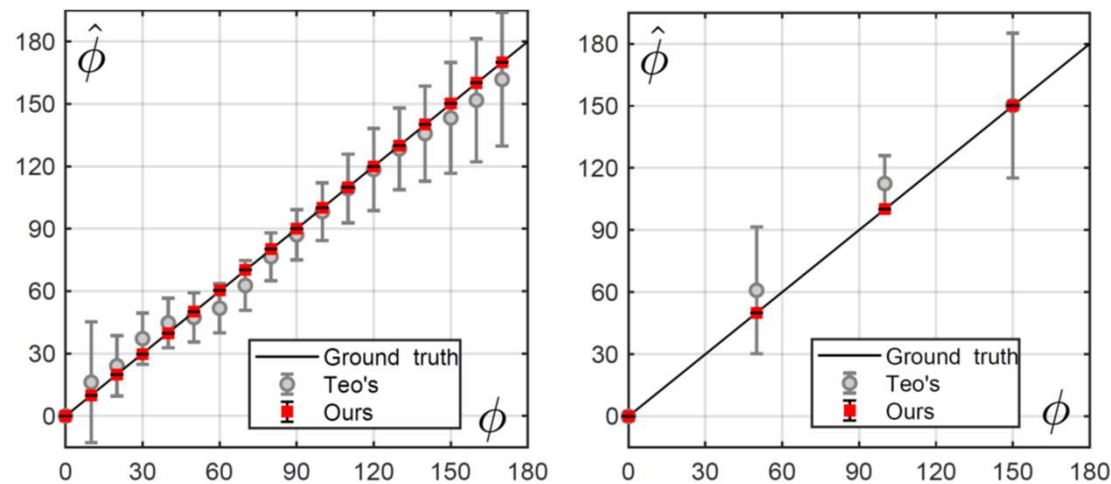


1. Our method performs well
2. Schechner's method is sensitive to initialization
3. Schechner's method is less reliable when $\# \phi$ is small, but our method is still robust

Experiments – Simulation

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Unknown CRF

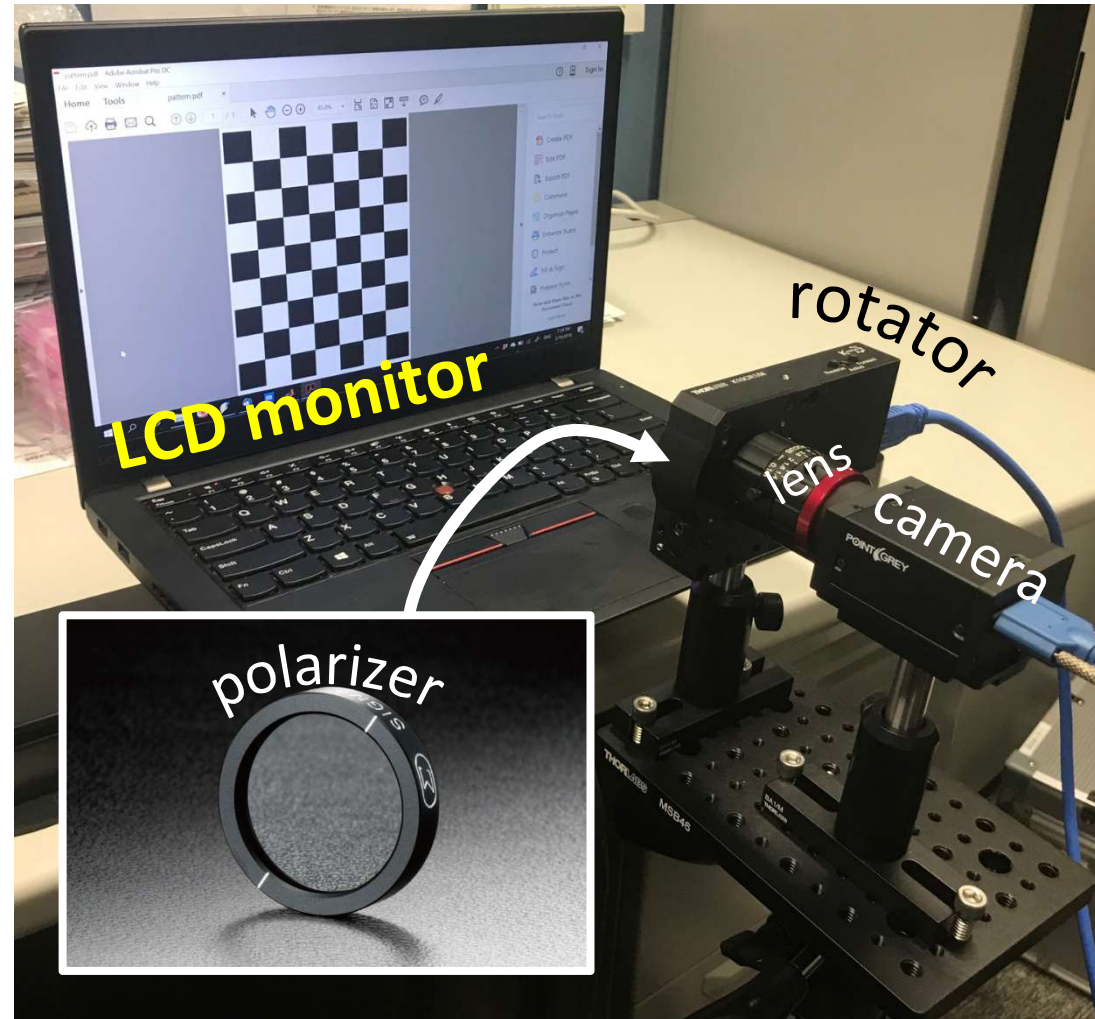


1. Our method performs well
2. Teo's method is sensitive to initialization
3. Teo's method is less reliable when $\# \phi$ is small, but our method is still robust

Experiments – Real-world

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Setup



Experiments – Real-world

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Environment illumination

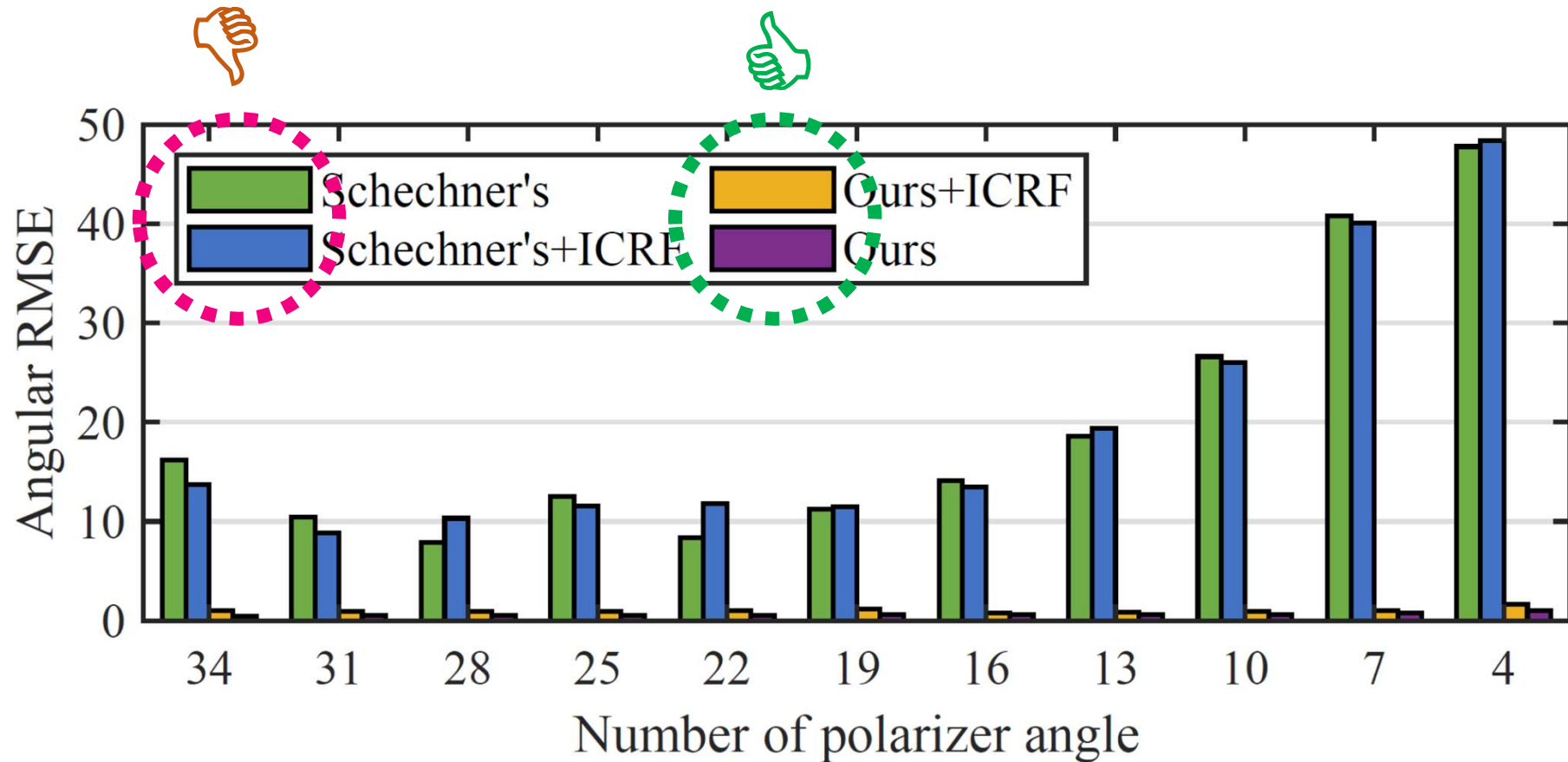
	Known ICRF		Unknown ICRF	
	CRF err.	Ang. err.	CRF err.	Ang. err.
Dark room	$\times$	0.76 ± 0.20	0.01 ± 0.01	0.48 ± 0.15
Bright room	$\times$	0.80 ± 0.28	0.05 ± 0.01	0.71 ± 0.11

- Reliably remove effect of environmental illumination
- The given ICRF could contain errors, but our joint method is good

Experiments – Real-world

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Effectiveness of using less polarizer angles



Experiments – Real-world

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Benefits of the adapted checker pattern P3

Known ICRF				Unknown ICRF		
	CRF err.	Ang. err.	#images	CRF err.	Ang. err.	#images
P0	✗	0.80±0.16	≥ 4	0.20±0.06	82.2±26.1	≥ 4
P1	✗	0.78±0.15	≥ 4	0.07±0.02	1.24±0.43	> 4
P2	✗	0.79±0.14	≥ 4	0.02±0.02	0.38±0.32	> 4 + 11
P3	✗	0.78±0.15	≥ 4	0.01±0.01	0.48±0.15	≥ 4

- **known ICRF**: standard checker pattern can achieve the same accuracy
- **unknown ICRF**: P1 suffers from *spatial inconsistency*
- **unknown ICRF**: more accurate but require more images
- **unknown ICRF**: our results is close to GT with less images

Experiments – Real-world

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Benefits of the adapted checker pattern P3

Known ICRF				Unknown ICRF		
	CRF err.	Ang. err.	#images	CRF err.	Ang. err.	#images
P0	✗	0.80 ± 0.16	≥ 4	0.20 ± 0.06	82.2 ± 26.1	≥ 4
P1	✗	0.78 ± 0.15	≥ 4	0.07 ± 0.02	1.24 ± 0.43	≥ 4
P2	✗	0.79 ± 0.14	≥ 4	0.02 ± 0.02	0.38 ± 0.32	$\geq 4 + 11$
P3	✗	0.78 ± 0.15	≥ 4	0.01 ± 0.01	0.48 ± 0.15	≥ 4

- Accurate estimated ICRF could be distorted during BA

Experiments – Real-world

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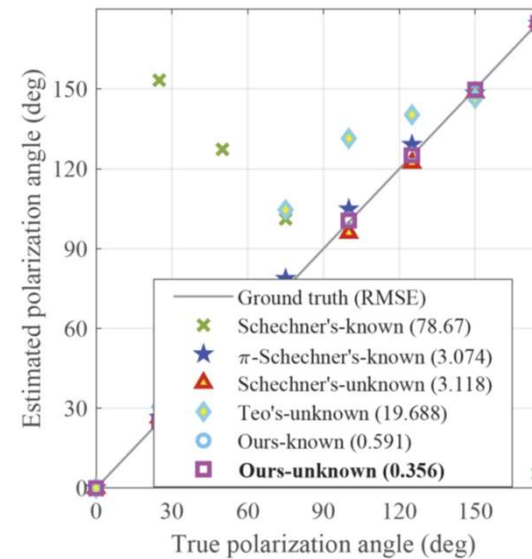
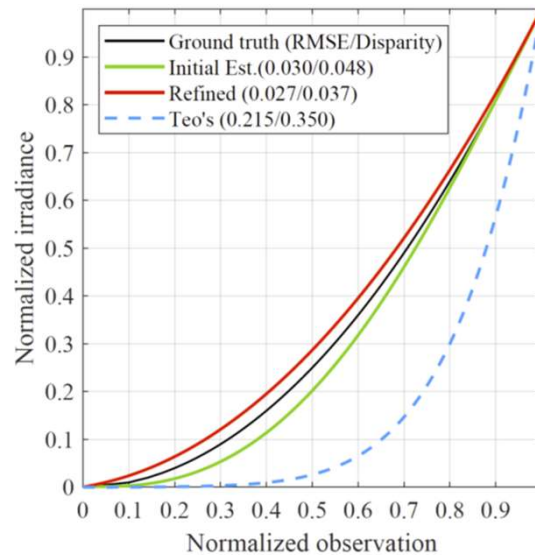
Joint calibration vs. separate calibration

	Known ICRF				Unknown ICRF			
	CRF err.	Ang. err.	ψ err.	#images	CRF err.	Ang. err.	ψ err.	#images
Separate	X	0.45	3.08	$\geq 4+2$	0.02	0.83	3.10	$\geq 4+2+11$
Joint	0.02	0.38	0.19	≥ 4	0.01	0.48	0.20	≥ 4
								

Experiments – Real-world

90

Comparison with the state-of-the-art methods

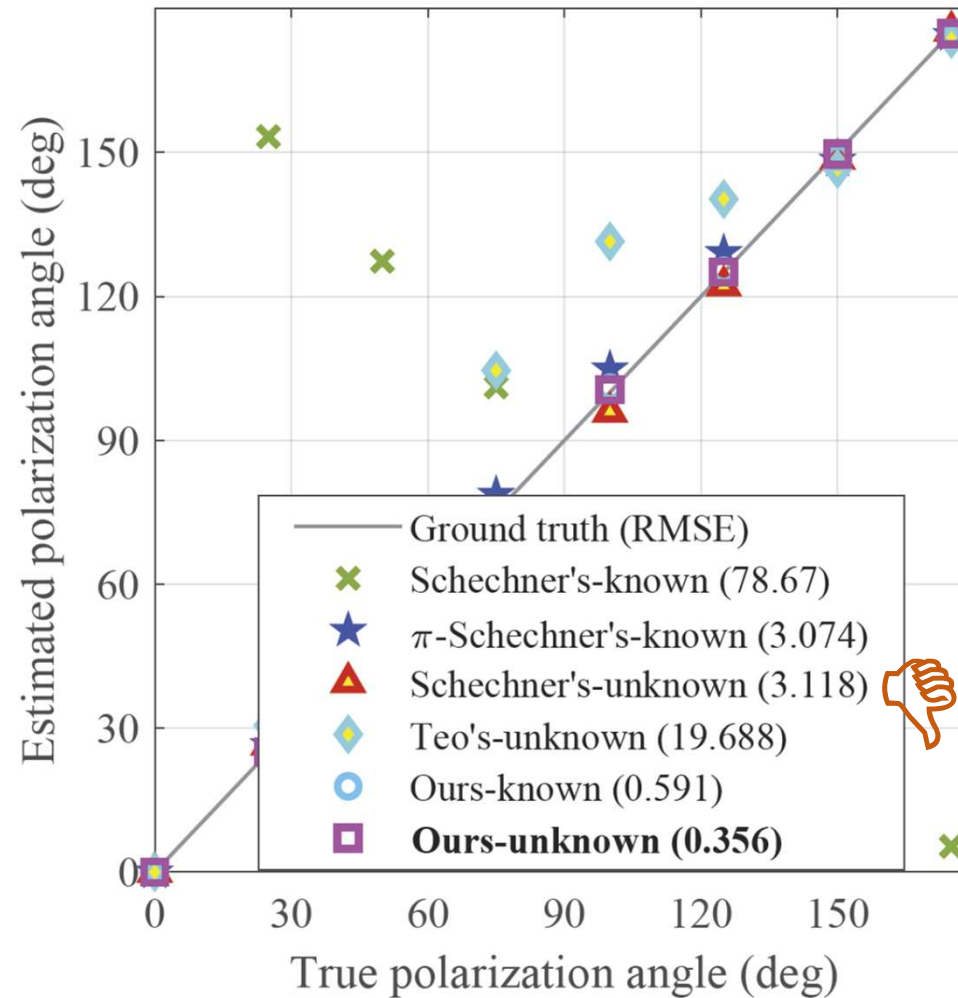


CRF	Method	CRF err.	Ang. err.	#polar. ang.	#images
known	[2]	$\times$	8.85 ± 15.39	≥ 4	≥ 4
	<i>Ours</i>	$\times$	0.62 ± 0.28	≥ 2	≥ 4
unknown	[2] + ICRF	$\times$	15.84 ± 29.59	≥ 4	$\geq 4 + 11$
	[3]	0.13 ± 0.09	12.56 ± 7.31	≥ 4	≥ 4
	<i>Ours</i>	0.04 ± 0.02	0.63 ± 0.18	≥ 2	≥ 4

Experiments – Real-world

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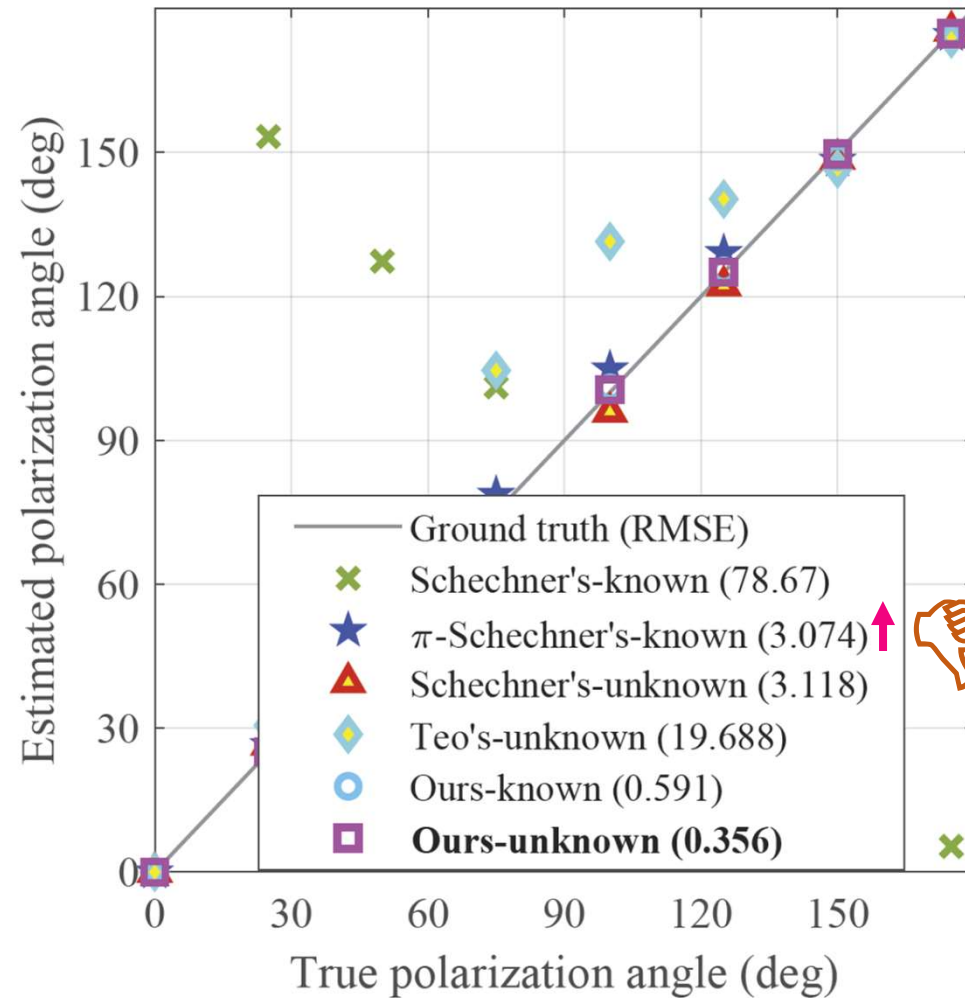
Comparison with the state-of-the-art methods



Experiments – Real-world

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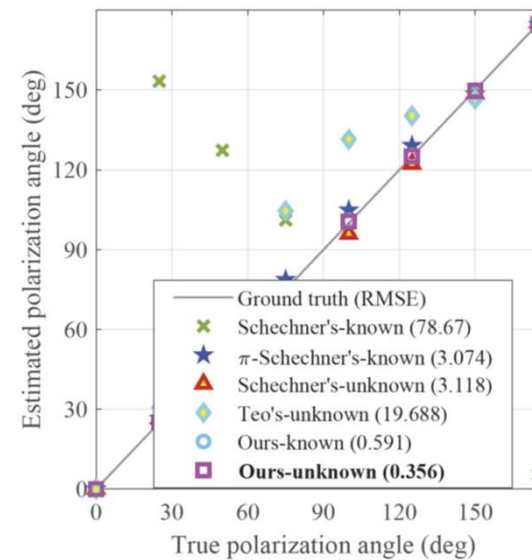
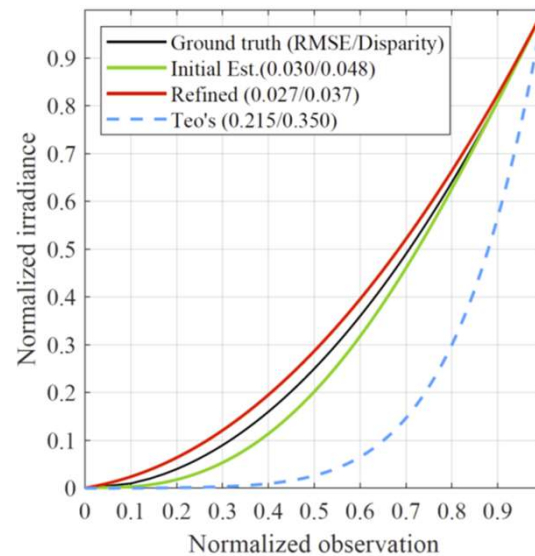
Comparison with the state-of-the-art methods



Experiments – Real-world

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Comparison with the state-of-the-art methods

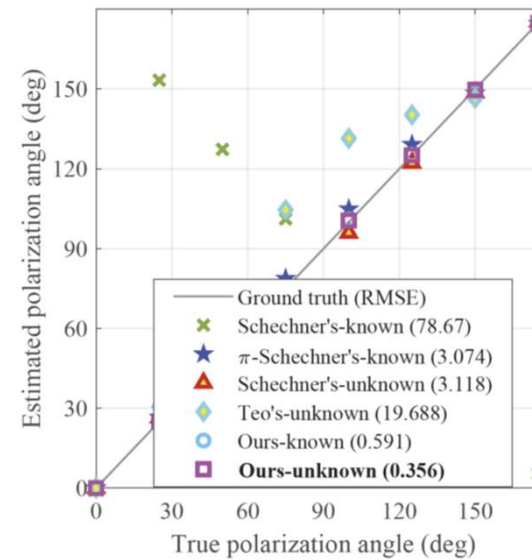
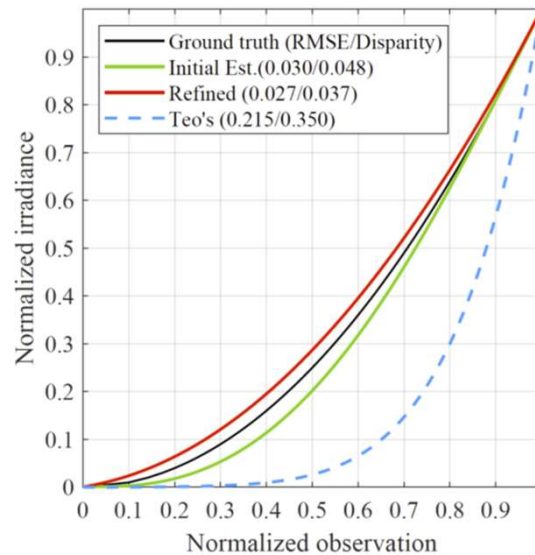


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Experiments – Real-world

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Comparison with the state-of-the-art methods

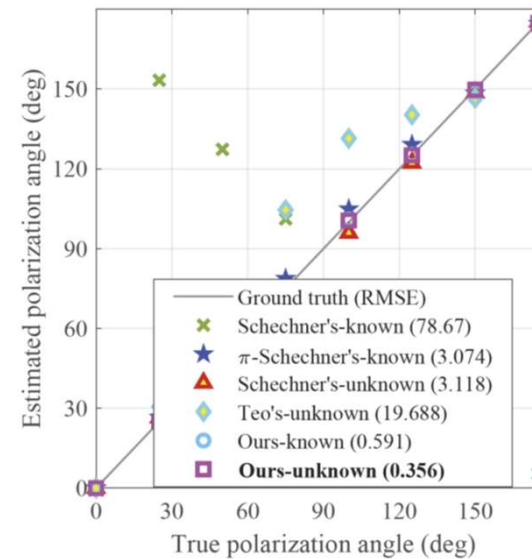
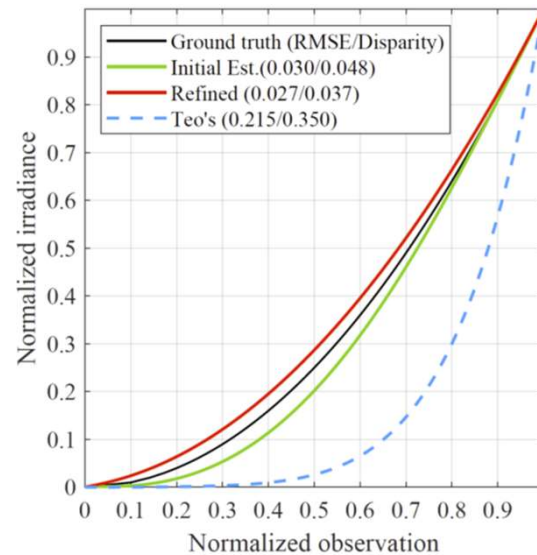


CRF	Method	CRF err.	Ang. err.	#polar. ang.	#images
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Experiments – Real-world

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Comparison with the state-of-the-art methods

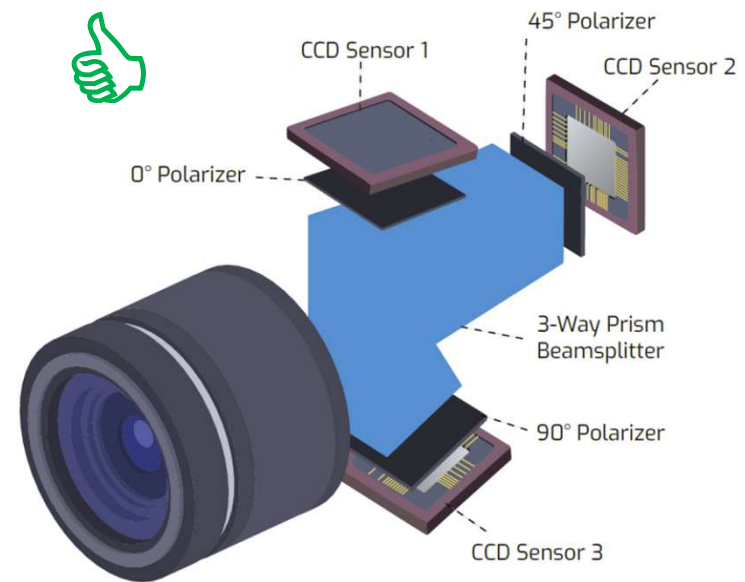
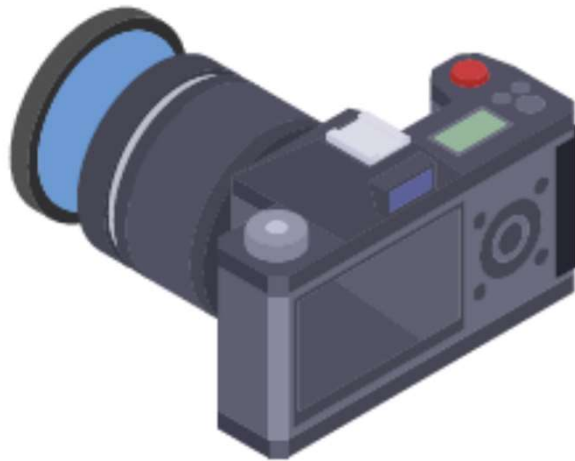


CRF	Method	CRF err.	Ang. err.	#polar. ang.	#images
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	[3]	0.13 ± 0.09	12.56 ± 7.31	≥ 4	≥ 4
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Discussion

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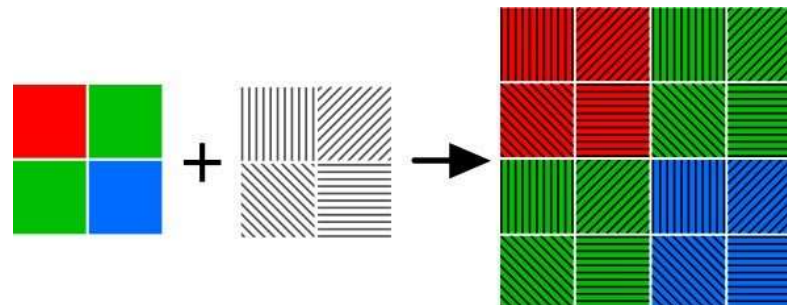
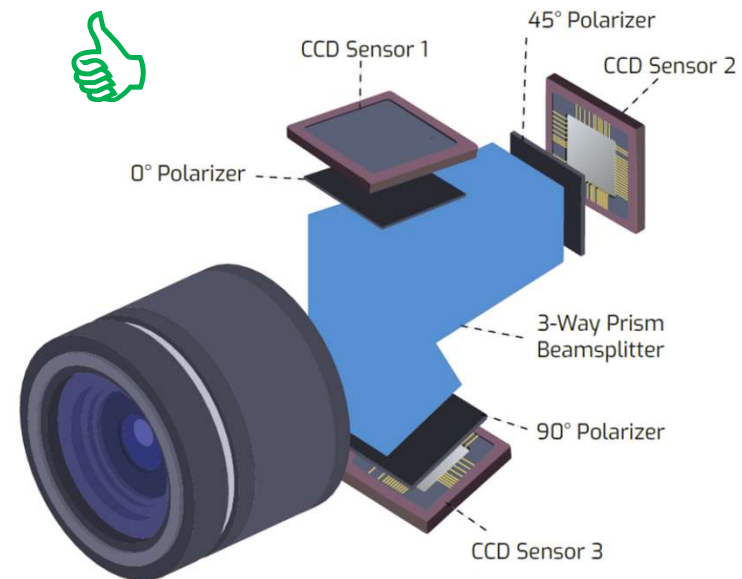
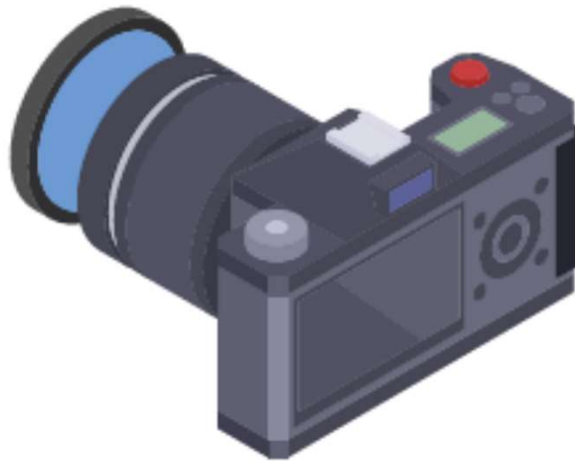
Applicability



Discussion

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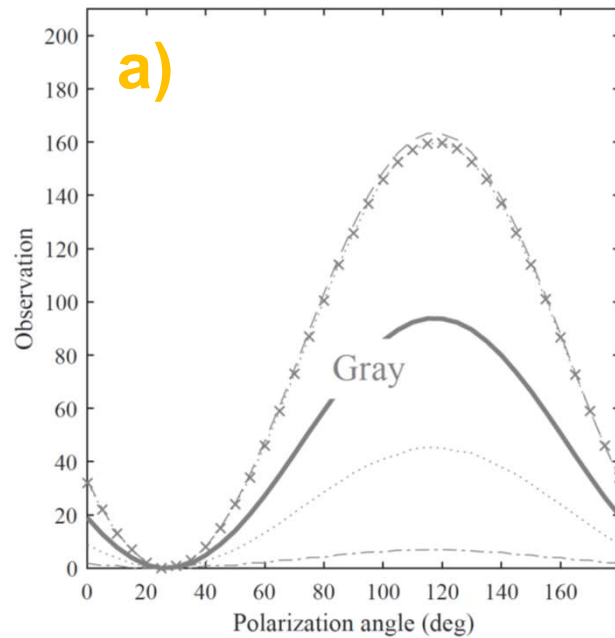
Applicability



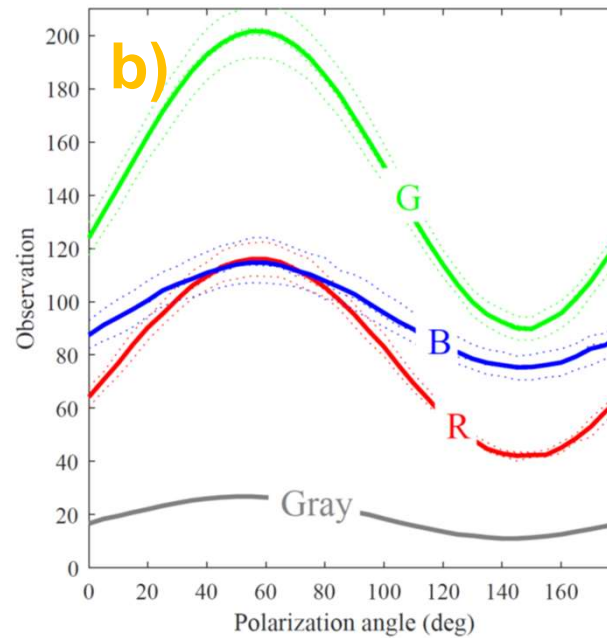
Discussion

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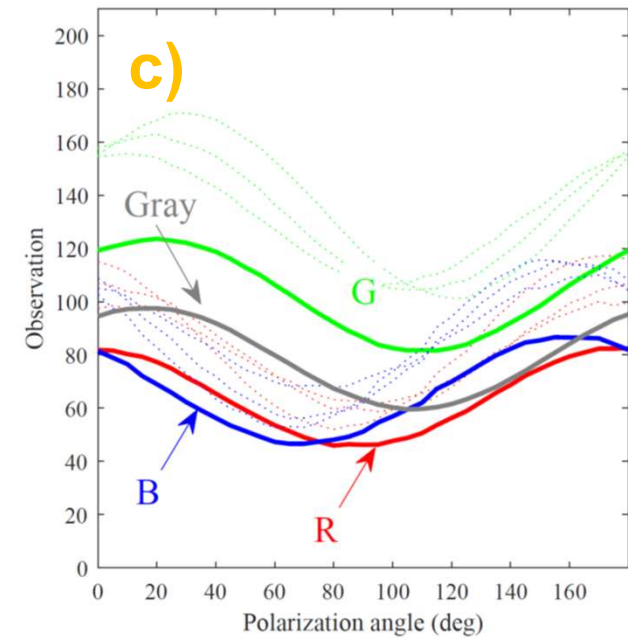
LCD screens with a touch panel



HUAWEI Meta 10 Lite



iPhone 6s



iPhone 7 Plus

Discussion

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Quick Test

Conclusion

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We propose a *joint* calibration method using characteristics of an LCD monitor.

- **Novel and new:** The basic idea of joint calibration with an LCD monitor is **novel**, and our linear polarization calibration method due to the characteristics of LCD monitors is **new**.
- **Efficient and effective:** Using the estimated CRF as initialization, our bundle adjustment leads to **accurate** and **reliable** results. Which is demonstrated by conducting **extensive experiments**. Considering that LCD monitors are everywhere, we believe that our method is **easy** to use as self-calibration methods.

Thank you!